



Satellite Remote Sensing Imagery Quality and Timeliness: Considerations for Use in Regional Estimation of Crop Production

Annually



Corn Planted Acreage Up Slightly from 2012
Soybean Acreage Up 1 Percent
All Wheat Acreage Up 1 Percent
All Cotton Acreage Down 17 Percent

40. *Redwood* planted area for 2013 is estimated at 19.3 million acres, 17 percent below last year, 18.0 million acres, down 17 percent from 2012. *American Pine* area is estimated at 228,000 a 2012.

ISSN: 1936-3737

Florida frozen concentrated orange juice (FCOJ) yield forecast for the 2013-2014 season is 42.0 degrees Brix, down 1 percent from the April forecast and down 1 percent from last season's 1.59 gallons per box. The early-midseason portion is projected at 1.52 gallons per box, up 1 percent from the April forecast and up 1 percent from last season's 1.51 gallons per box. The Valencia portion is projected at 1.64 gallons per box, down 1 percent from the April forecast and down 1 percent from last season's 1.64 gallons per box. All projections of yield assume the processing relationships this season will be similar to those of the previous several seasons.

Monthly

ISSN: 1946-3007

[These 18 States planted 91% of the 2013 corn acreage]

- Represents zero

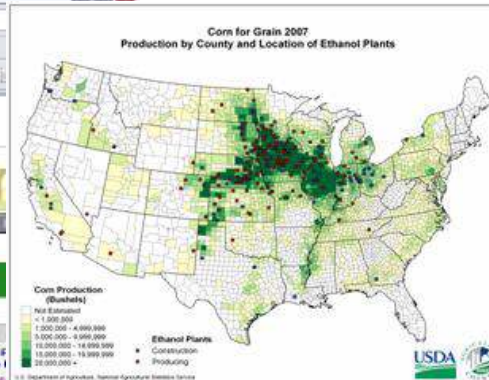
[These 18 States planted 91% of the 2013 corn acreage]

- Represents zero

Weekly

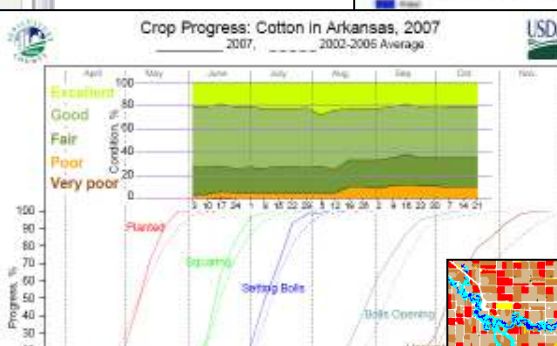
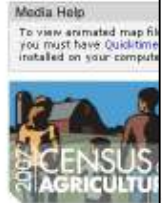
NASS Research and Development Division

Spatial Analysis Research Section



Also See

- Research & Associate
- Seasonal Progress and Condition
- Recently Sensed Data
- Crop Acreage
- Crop Yield
- Future Vision



Spatial Data

Vegetation Condition Images

Cropland Data Layer

Image Gallery (2002) available for these states: Arkansas, Illinois, Indiana, Iowa, N. Dakota, Mississippi, Missouri, Nebraska, Wisconsin

Land Use Strata for Selected States

Census of Agriculture

2002 Census Map Gallery

2002 Maps: Gallery | Star Tree | Link

Interact with Data (1997)

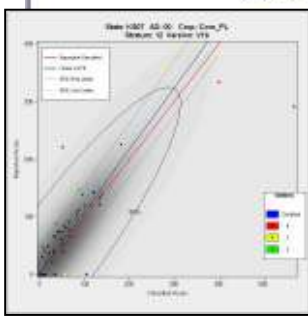
Linked Micromap Plots (1997): Corn | Cotton | Hay | Soybeans | Wheat

Animated Maps

Crop Acreage

Vegetation Condition

Corn | Cotton | Data Soybeans | Wheat



Reports and Presentations

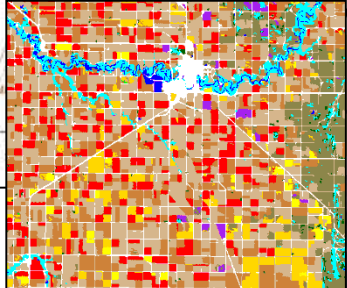
733 archived reports available: GIS | Survey | Yield

Star Tree Diagram

Presenter

Last modified

Statistics System (SPSS) | Site Information Statement



Land cover mapping - Cropland Data Layer (CDL)

Agriculture

Pasture/Grass
Corn
Soybeans
All Wheat
Other Hay

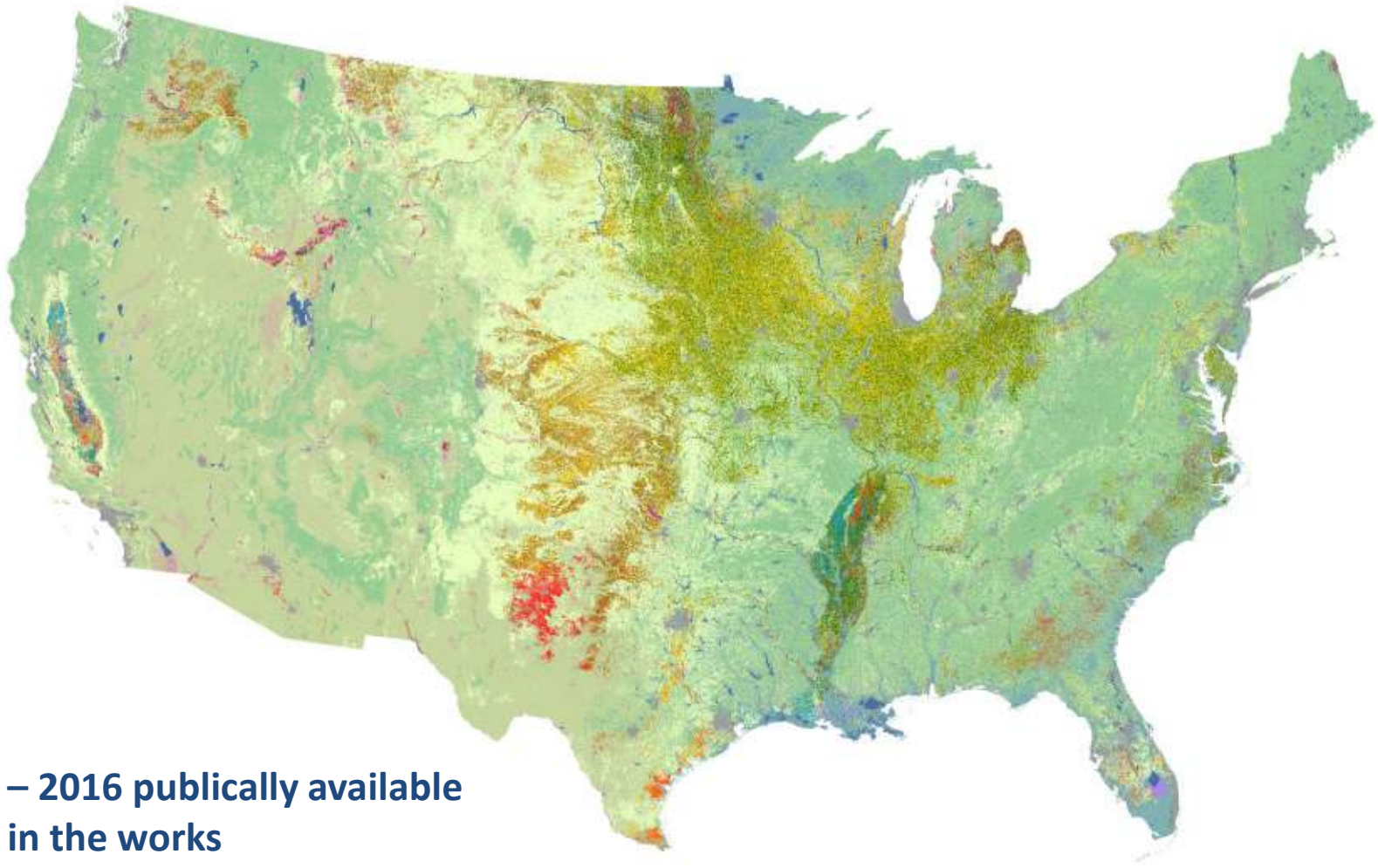
Fallow/Idle Cropland
Alfalfa
Cotton
Other Crops
Vegetables/Fruits/Nuts

Sorghum
Other Small Grains
Rice

Non-Agriculture

Woodland
Shrubland
Urban/Developed
Wetlands
Water

Barren
Perennial Ice/Snow



* 2008 – 2016 publically available

* 2017 in the works

* 2008 and 2009 being reprocessed from 56m to 30m

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Celebrating 45 Years of Landsat 1972-2017

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Landsat represents the world's longest continuously acquired collection of space-based moderate-resolution land remote sensing data.

[Download Data Now!](#)

Landsat Headlines

November 29, 2017

November 29, 2017 - Delivery changes to Band 4 Solar/Sensor Zenith/Azimuth Angle Bands

A recent software release to the Earth Resources Observation and Science (EROS) Center Science Processing Architecture (ESPA) on-demand interface changes the delivery to users of the Band 4 Solar/Sensor zenith/azimuth angle bands.

November 21, 2017

November 21, 2017 - Landsat Analysis Ready Data for Alaska and Hawaii Available

USGS Landsat Analysis Ready Data (ARD) for Alaska and Hawaii are now available for download from EarthExplorer. This completes the release of U.S. Landsat ARD for all 50 states. [\(Read More\)](#)

November 08, 2017

November 8, 2017 - New Video Introduces Landsat Analysis Ready Data

A new video introducing Landsat Analysis Ready Data (ARD) has been added to the Landsat ARD webpage, as well as the Landsat Media Library. [\(Read More\)](#)

November 01, 2017

November 1, 2017 - Upcoming Infrastructure Maintenance

On **Tuesday, November 7, 2017**, the USGS EROS Center in Sioux Falls, South Dakota will temporarily halt Landsat data processing at 11:00 am CST, and all data distribution from EarthExplorer, GloVis, the LandsatLook Viewer, and ESPA at 3:00 pm CST due to planned required infrastructure maintenance.

October 30, 2017

October 30, 2017 - Landsat Analysis Ready Data Available

USGS Landsat Analysis Ready Data (ARD) for the conterminous United States are now available for download from EarthExplorer. [\(Read More\)](#)

Landsat Missions | GloVis

Secure | https://glovis.usgs.gov

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GloVis

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Interface Controls

Choose Your Data Set(s)

Data Set Filter

☐ Landsat 1-5 MSS

☐ Landsat 4-5 TM C1 Level-1

☐ Landsat 7 ETM+ C1 Level-1

☒ Landsat 8 OLI/TIRS C1 Level-1
133 scenes match your criteria

☐ OrthoView-3

☐ Sentinel-2

Metadata Filter

Date Range
mm/dd/yyyy to mm/dd/yyyy

Cloud Cover
0-100 or empty to 0-100 or empty

Months
Jan Feb

APPLY CLEAR

Selected Scenes (0)

Lat: 39.5464, Lon: -73.7732

Richmond

30 ym
30 mi

Landsat 8 OLI/TIRS C1 Level-1
LC08_L1TP_015003_20171126_20171126_01_RT
Acquired on 2017-11-26
Current Scene Browse Opacity (100%)

PREVIOUS SELECT NEXT

Leaflet | Map data © OpenStreetMap contributors, USGS, ERDC

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Page Last Modified: 06/10/2017



LandSat Viewer | QGIS

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GloVis Page Expires in 1:54:52

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Interface Controls

Choose Your Data Set(s)

Data Set Filter

- ☐ Landsat 1 MSS 8
- ☐ Landsat 4-5 TM CT Level 1 8
- ☐ Landsat 7 ETM+ CT Level 1 8
- ☒ Landsat 8 OLI/TIRS-C1 Level 1 8
233 scenes match your criteria
- ☐ OLI/TIRS 2 8
- ☐ Sentinel 2 8

Metadata Filter

Date Range
week00/yyyy to week00/yyyy

Cloud Cover
0-100 or empty to 0-100 or empty

Woods
User Filter

APPLY CLEAR

Selected Scenes (3)

Lat: 28.1988, Lon: -77.3780

Zoom

Full Screen

LandSat 8 OLI/TIRS-C1 Level 1
LC08_L1TP_2015012_20170622_20170912_01_T1
Acquired on 2017-09-22

Current Scene Browse Capabilities (100%)

PREVIOUS SELECT NEXT

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Page Accessed: 2017-11-22T04:01:26-06:00
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Page Last Modified: 08/15/2017

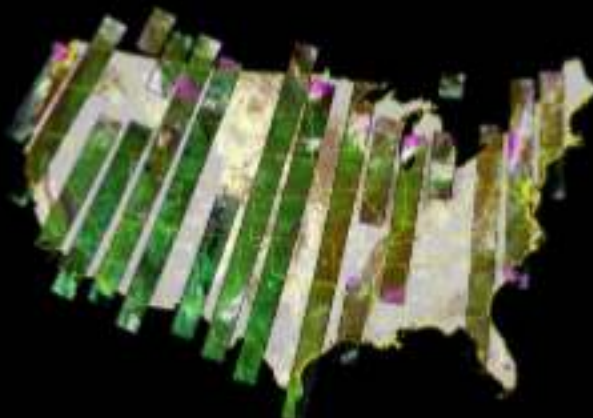
USA.gov

2017: June 16 – 22

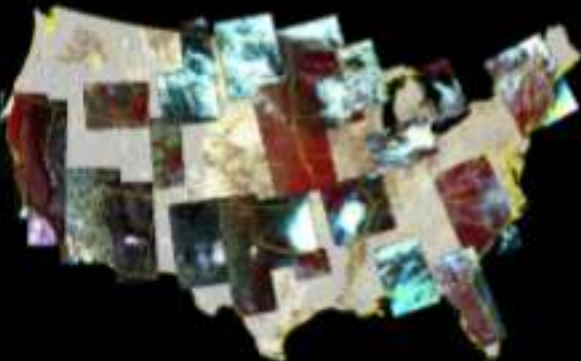
Agricultural areas



Landsat 8



Sentinel 2a



DMC Deimos



DMC UK2



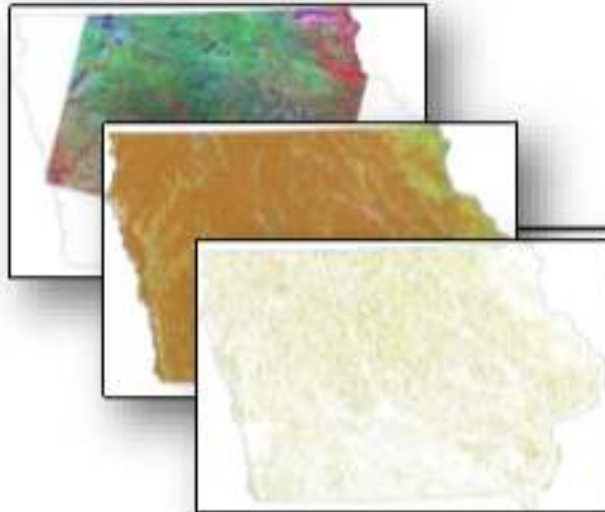
Resourcesat-2 LISS3

Available satellite imagery 2017: June 16 – 22



CDL Processing Flow

Input Data



Sampling



See5



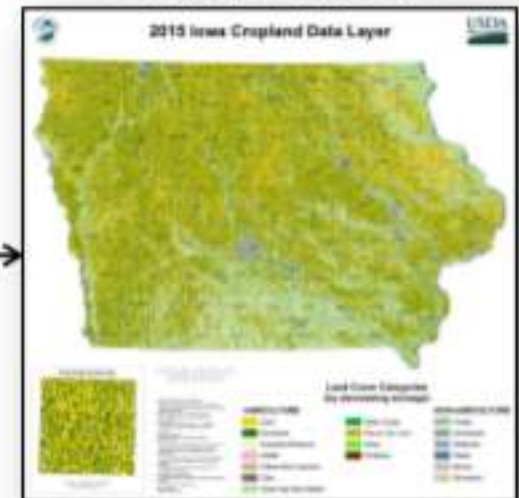
Decision Tree



Classification

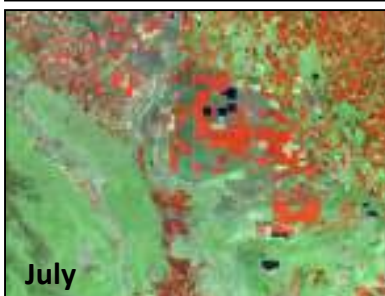
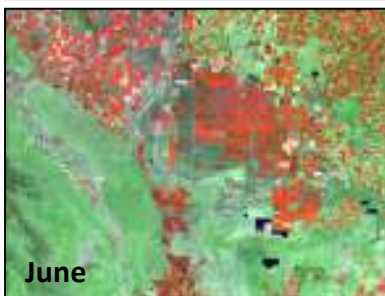
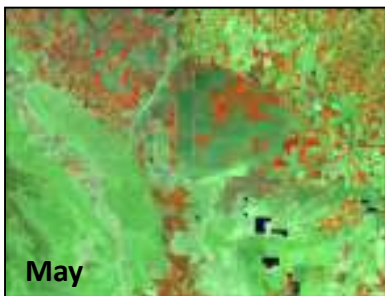
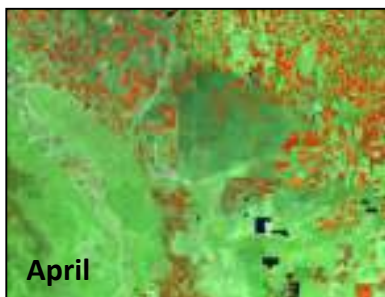


Output – ArcGIS



Classification

False Color IR Imagery

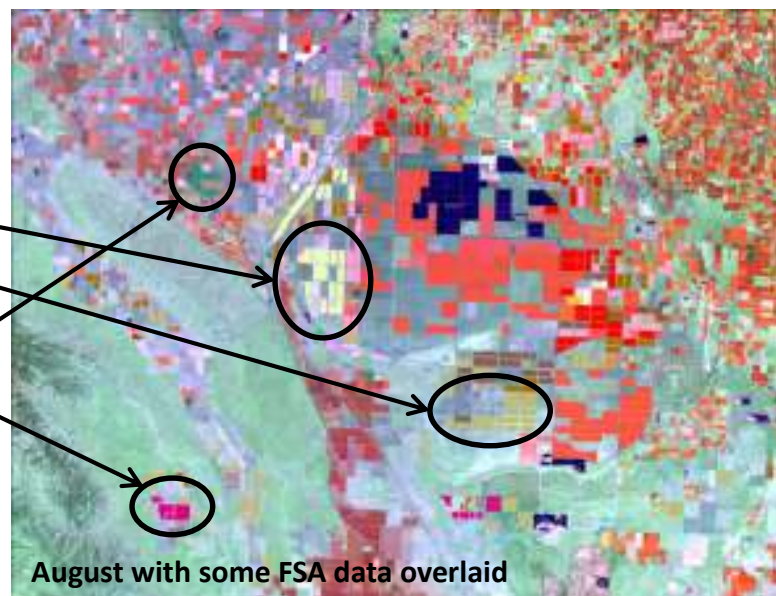


FSA Ground Truth

Land Cover Categories

Agriculture

- Pasture/Grass
- Alfalfa
- Fallow/Idle Cropland
- Winter Wheat
- Barley
- Cotton
- Almonds
- Corn
- Durum Wheat

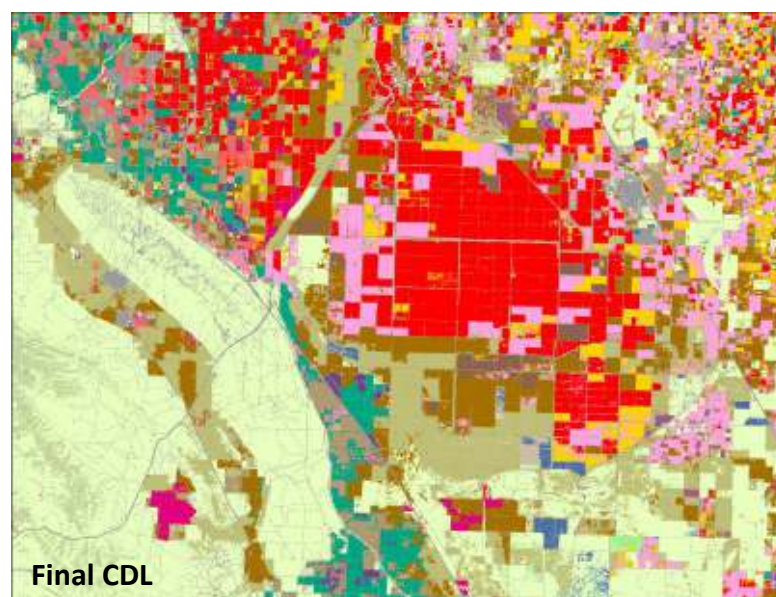


Final Classification

Land Cover Categories

Agriculture

- Pasture/Grass
- Alfalfa
- Fallow/Idle Cropland
- Winter Wheat
- Barley
- Cotton
- Almonds
- Corn
- Durum Wheat



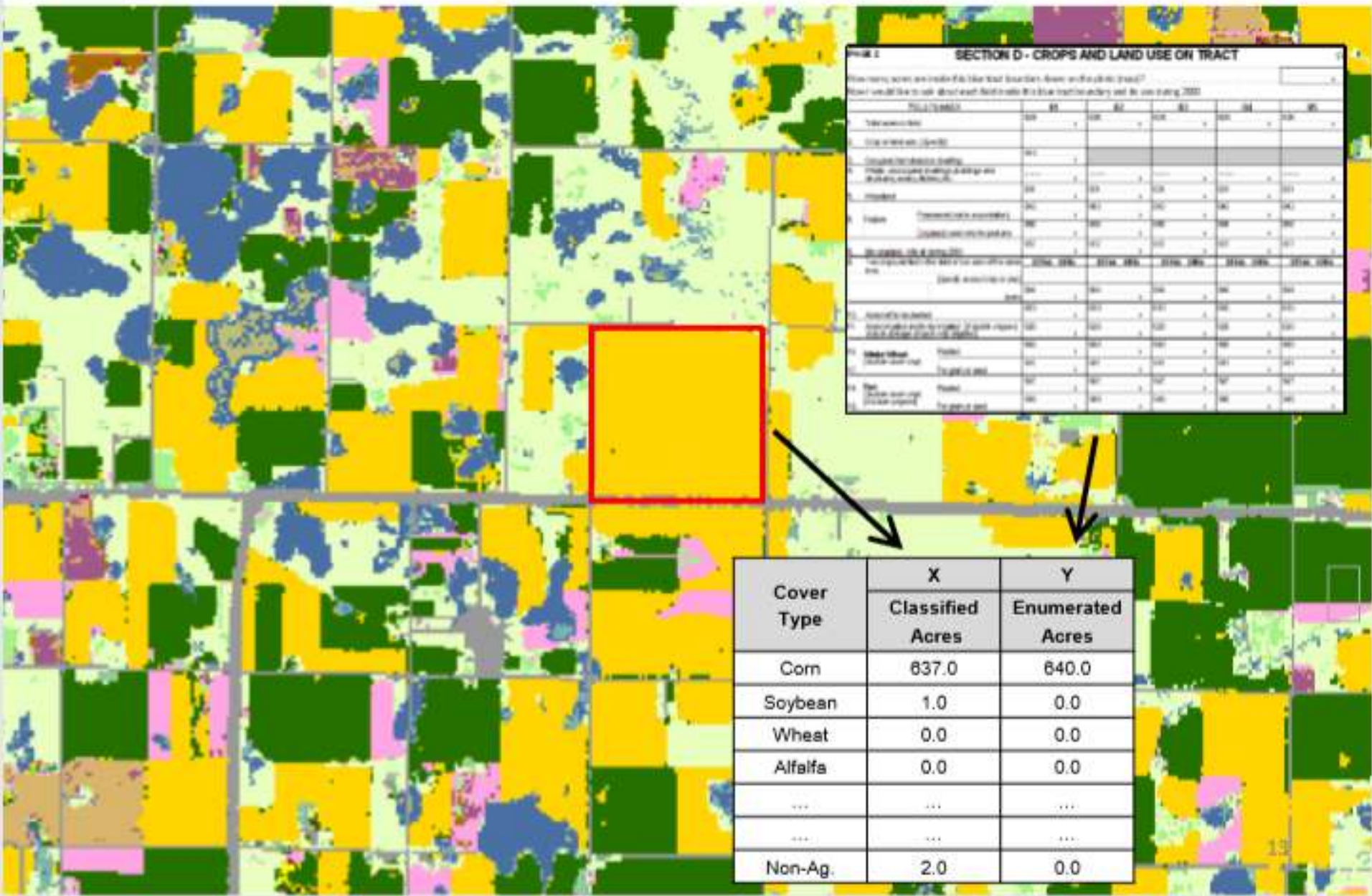
Accuracy Assessments

USDA, National Agricultural Statistics Service, 2014 **Colorado** Cropland Data Layer
STATEWIDE AGRICULTURAL ACCURACY REPORT

Crop-specific covers only	*Correct	Accuracy	Error	Kappa
-----	-----	-----	-----	-----
OVERALL ACCURACY**	2,630,488	85.5%	14.5%	0.812

Cover	Attribute	*Correct	Producer's	Omission		User's	Commission	Cond'l
Type	Code	Pixels	Accuracy	Error	Kappa	Accuracy	Error	Kappa
----	----	-----	-----	-----	-----	-----	-----	-----
Corn	1	419737	90.76%	9.24%	0.895	90.22%	9.78%	0.889
Sorghum	4	83214	62.32%	37.68%	0.611	64.72%	35.28%	0.635
Soybeans	5	1058	43.25%	56.75%	0.432	72.47%	27.53%	0.724
Sunflower	6	5760	39.64%	60.36%	0.395	70.61%	29.39%	0.705
Barley	21	7176	71.52%	28.48%	0.715	81.00%	19.00%	0.810
Winter Wheat	24	1100020	93.26%	6.74%	0.905	94.21%	5.79%	0.918
Millet	29	75109	67.86%	32.14%	0.671	76.85%	23.15%	0.762
Alfalfa	36	196153	89.75%	10.25%	0.891	85.60%	14.40%	0.848
Other Hay/Non Alfalfa	37	84626	63.33%	36.67%	0.624	85.92%	14.08%	0.854
Sugarbeets	41	4679	63.13%	36.87%	0.631	90.28%	9.72%	0.903
Dry Beans	42	9406	62.72%	37.28%	0.626	69.54%	30.46%	0.694
Potatoes	43	6104	89.74%	10.26%	0.897	93.79%	6.21%	0.938
Fallow/Idle Cropland	61	625989	88.08%	11.92%	0.855	89.23%	10.77%	0.869

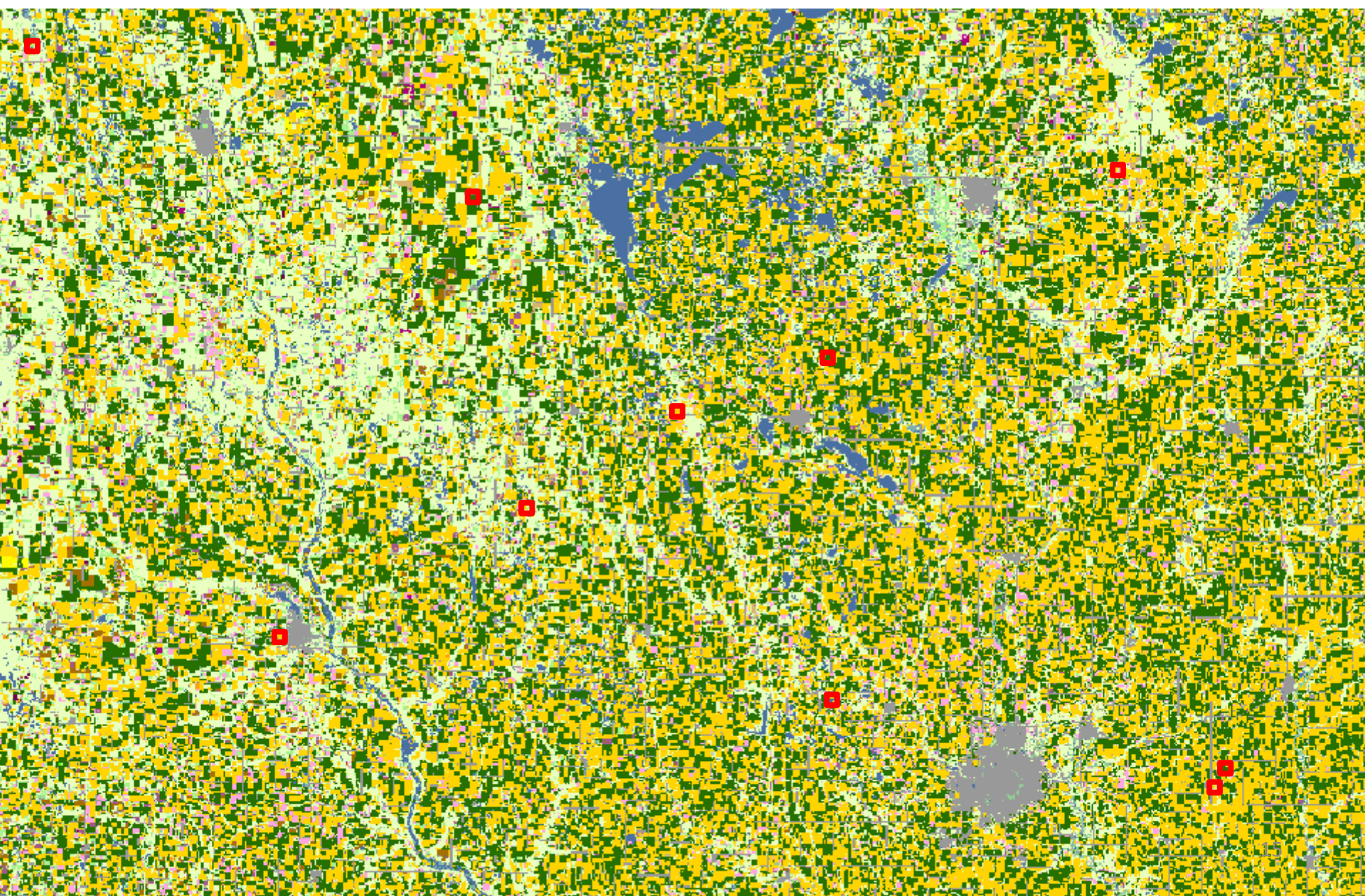
Classified area vs June enumerated



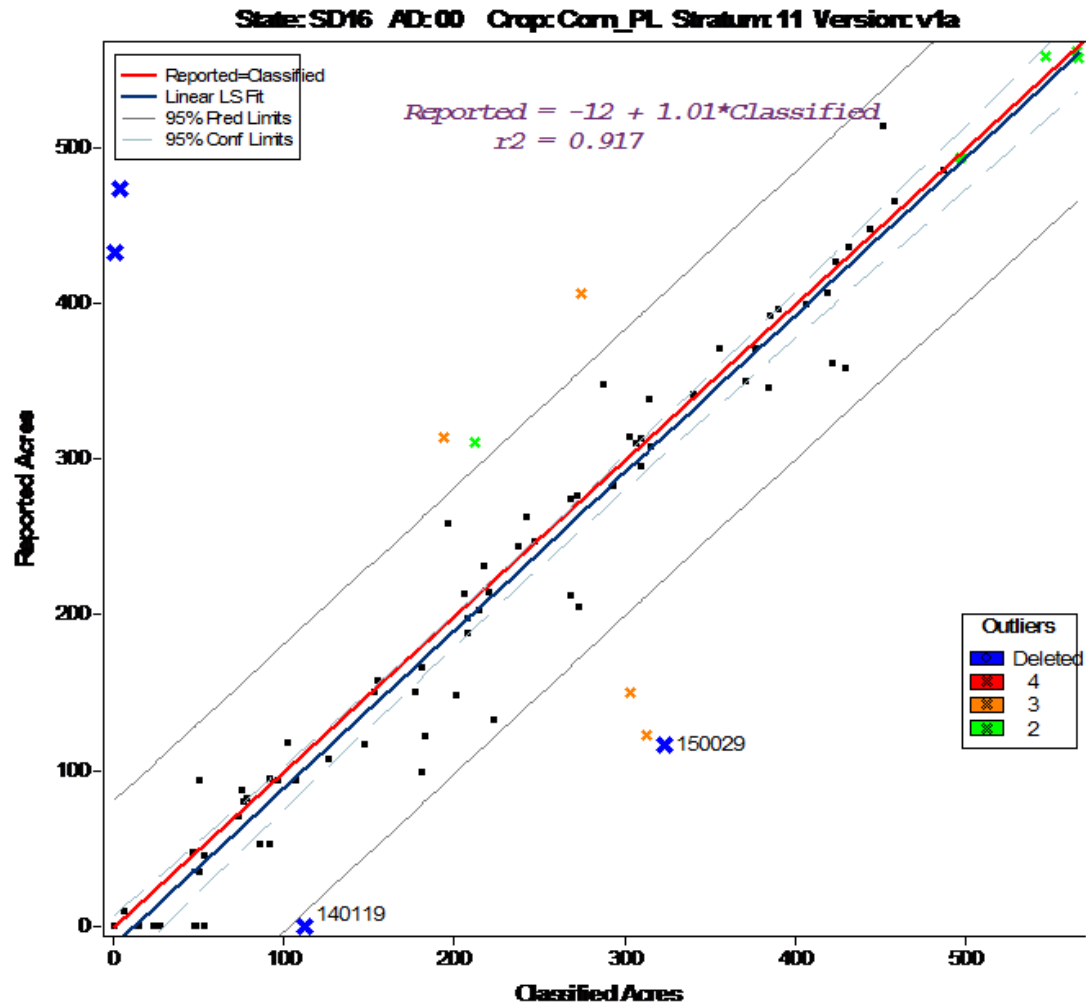
At three sites



10 sites and so forth....



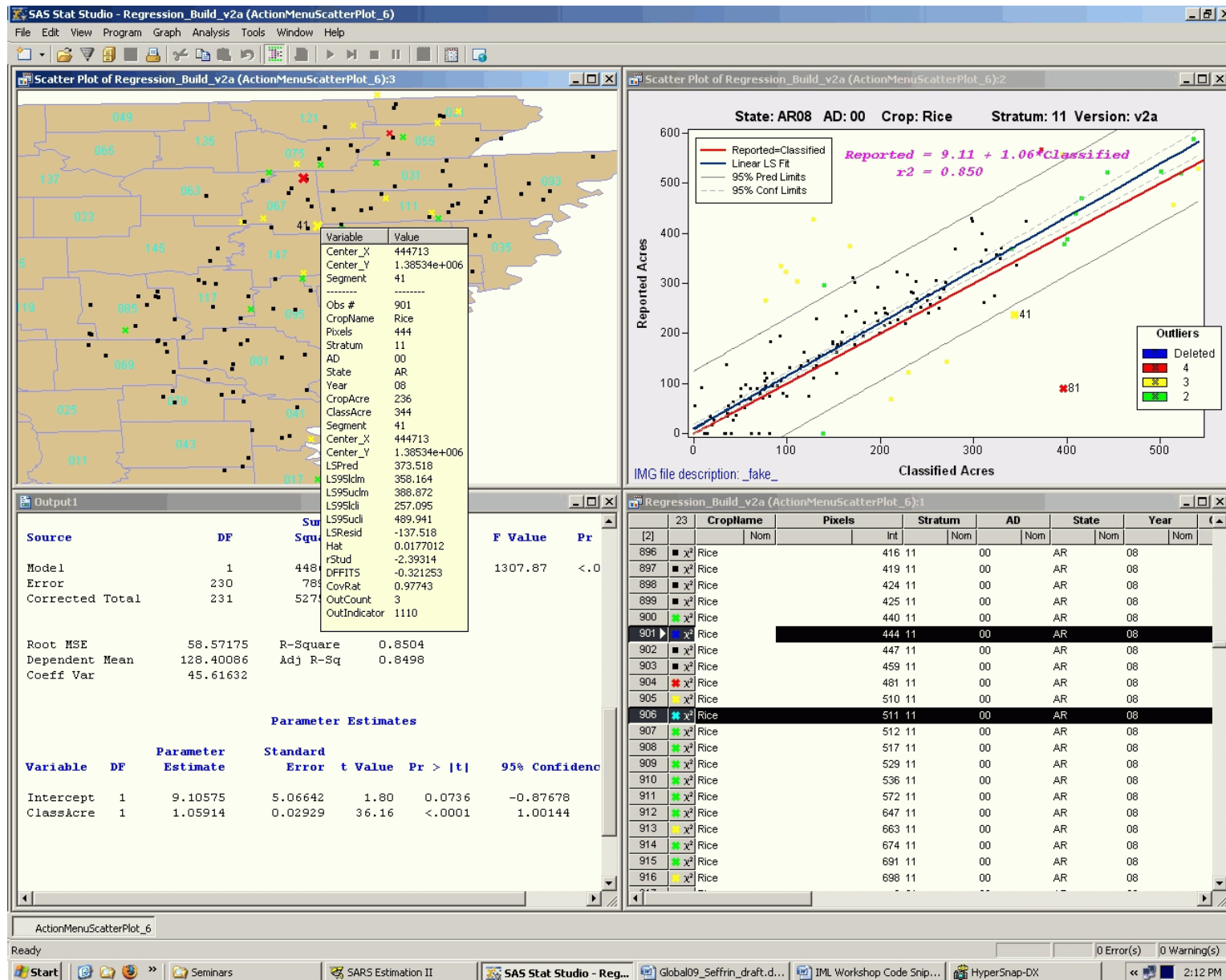
Acreage Regression Estimation



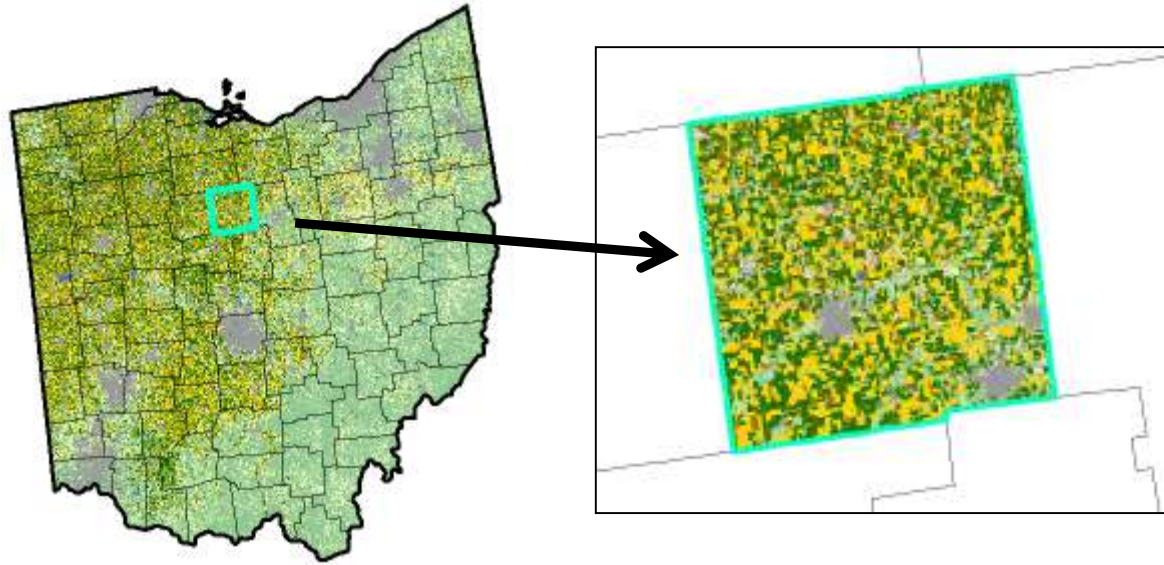
IMGfiledescription: _oct_subset_30m_

We don't just "pixel count" from CDL to estimate acreage

SAS-based Regression Estimate system



à la Bob Seffrin



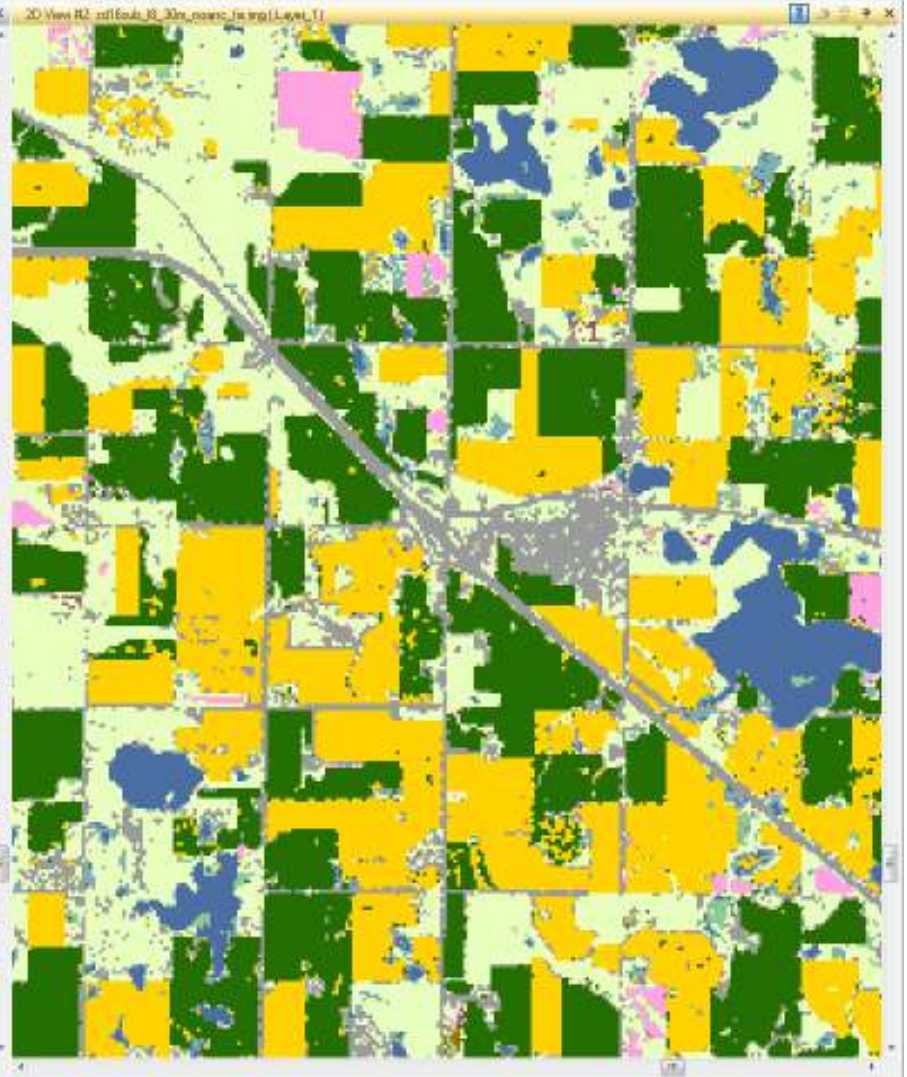
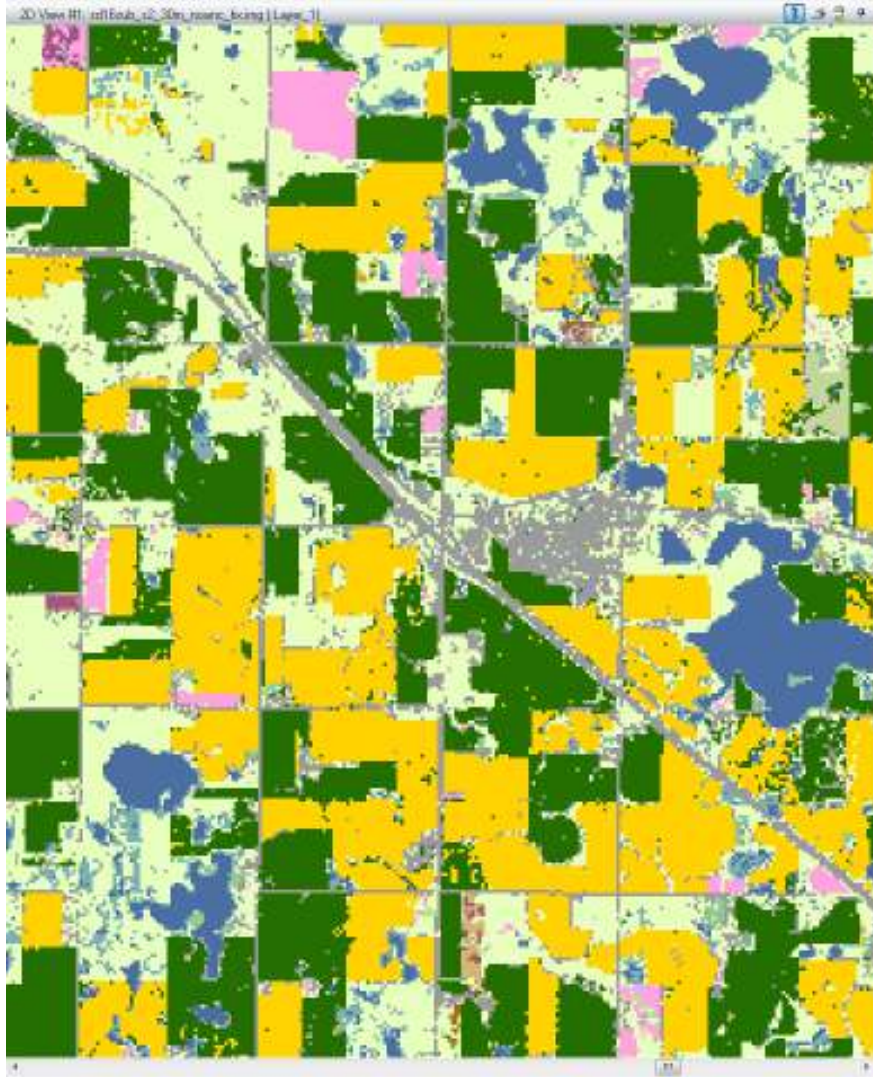
County Estimates

- Use Battese-Fuller estimator with nested design
- Apply state-strata level regression parameters
- Adjust intercept based on segments in county
- Ag Statistics Districts Est = Sum of County Estimates

Classification comparison #1

30m Sentinel-2a

30m Landsat 8



Classification comparison #2

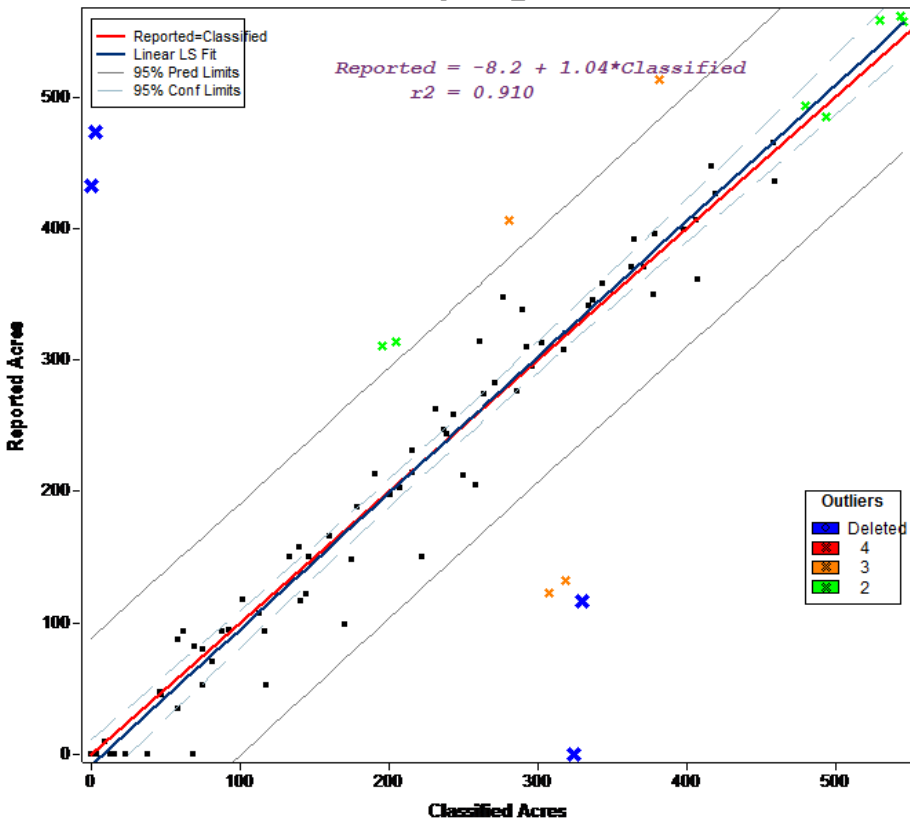
10m Sentinel-2a

15m Sentinel-2a



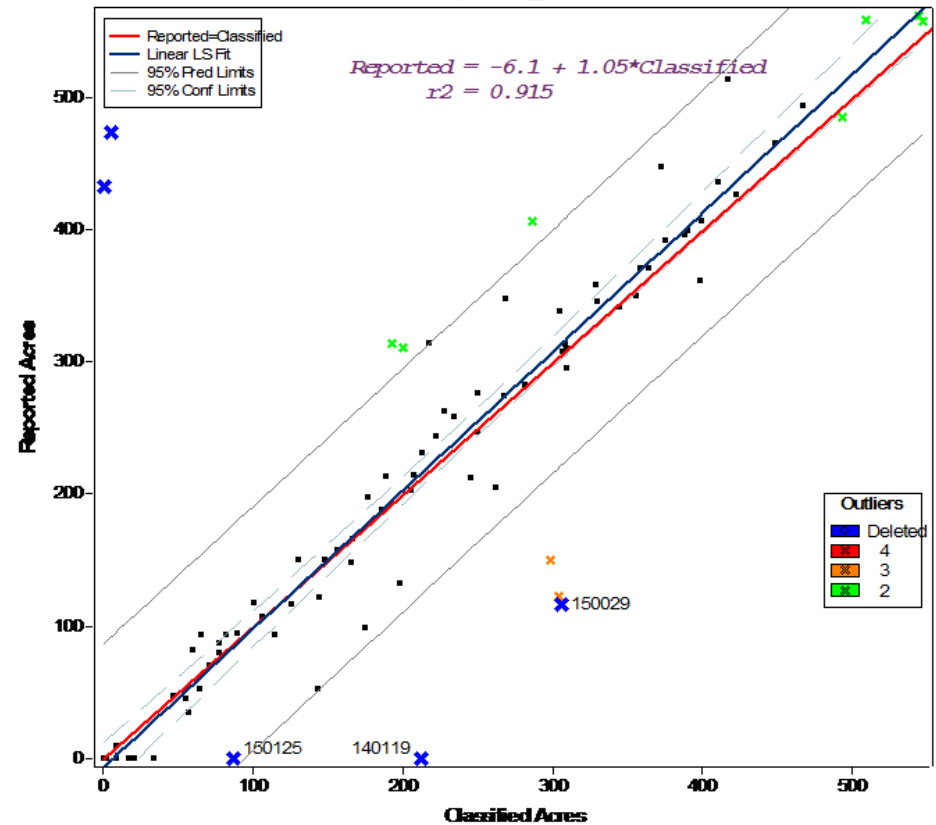
60m vs 15m regression analysis - corn

State: SD16 AD: 00 Crop: Corn_PL Stratum: 11 Version: v1a



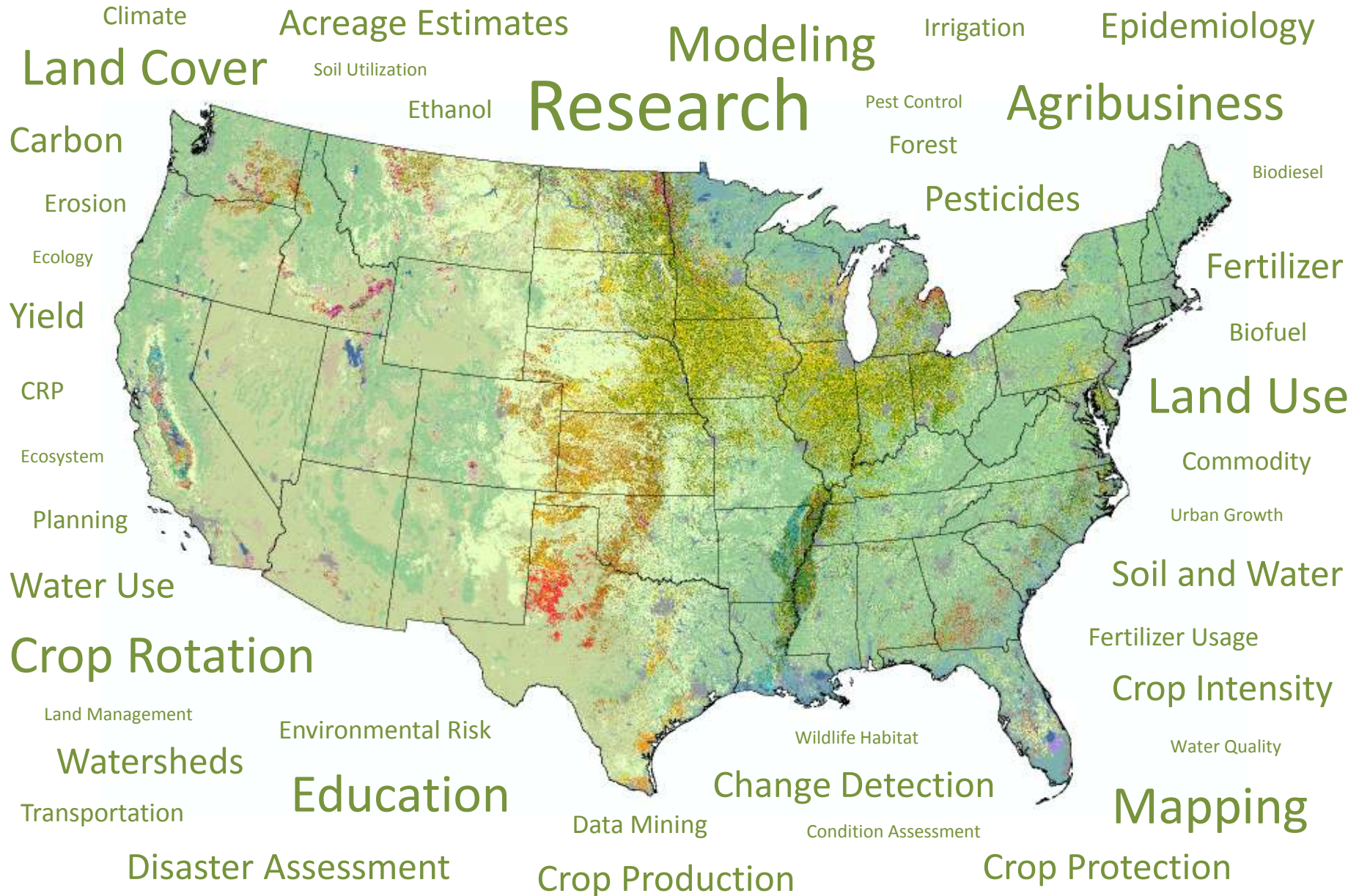
IMG file description: 60m_for_

State: SD16 AD: 00 Crop: Corn_PL Stratum: 11 Version: v3a

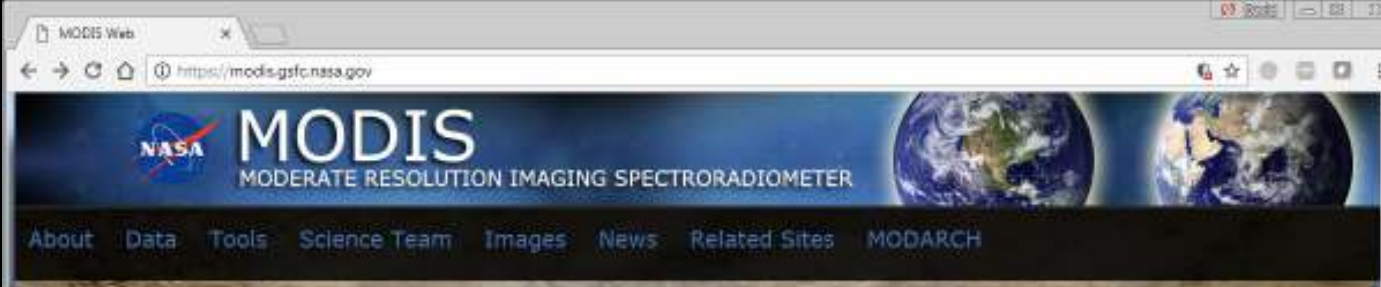


VG file description: sub_s2_15m_noan

CDL Applications







[Learn More About Today's Image](#)

A weather system that brought rain to Tehran and Iran's Caspian Sea coastline and Alborz mountains helped raise dust inland in late November, 2017...

[Continue Reading](#)

Data

The MODIS Data section contains everything from ATBDs to Product Descriptions to Product ordering information, including from Direct Broadcast data providers. Visit the Data section for more information.

[Learn More About MODIS Data](#)

News

[LP DAAC Announces Release of MODIS Version 6 Net Evapotranspiration Products](#)

[Release of NASA MEaSUREs CAMEL 5 km Products Announced By LP DAAC](#)

[View More MODIS News](#)

Tools

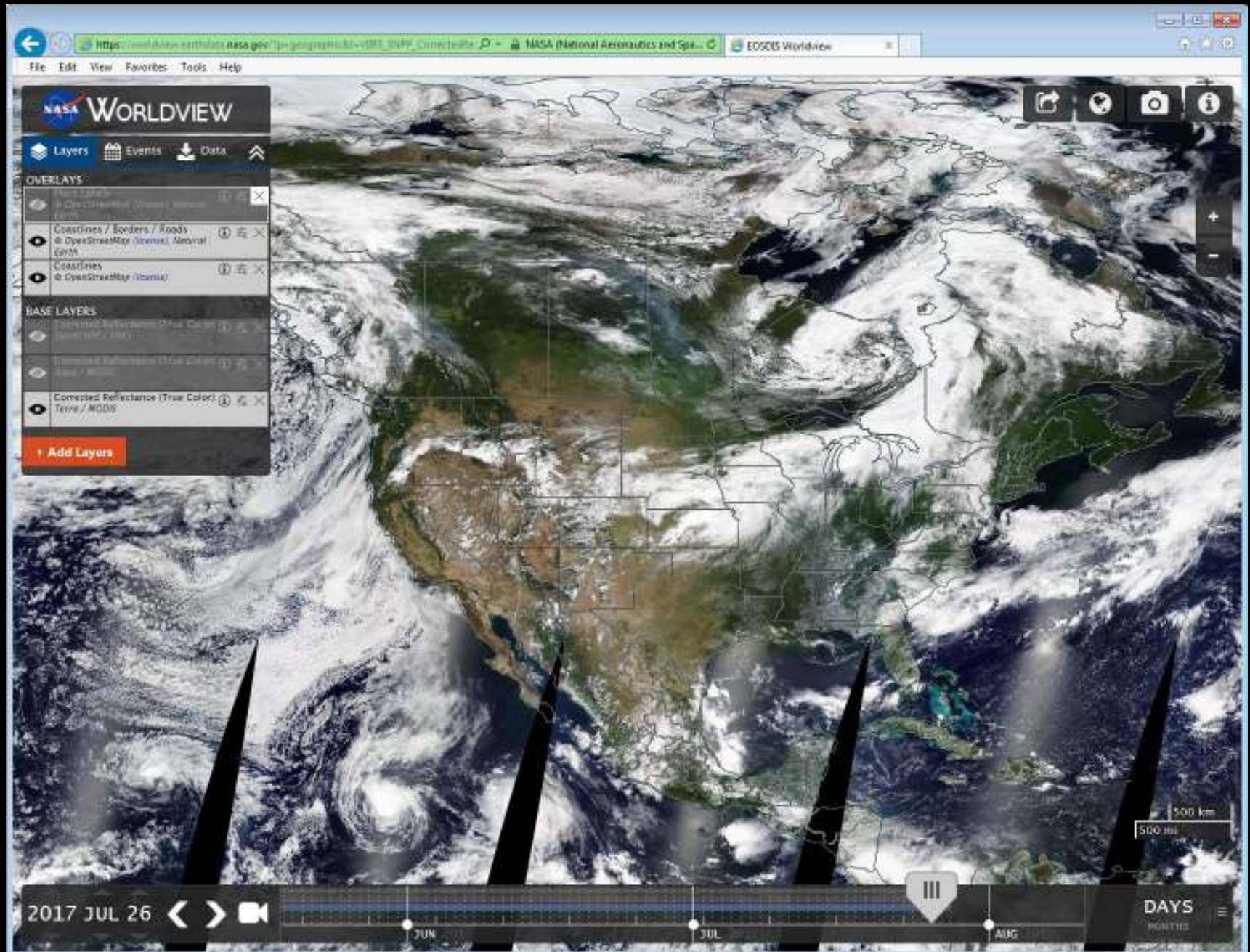
The MODIS Tools section has a complete listing of web-based tools that can be used to access a wide variety of MODIS Data, along with an array of links and a summary of each tool.

[Learn More About MODIS Tools ->](#)

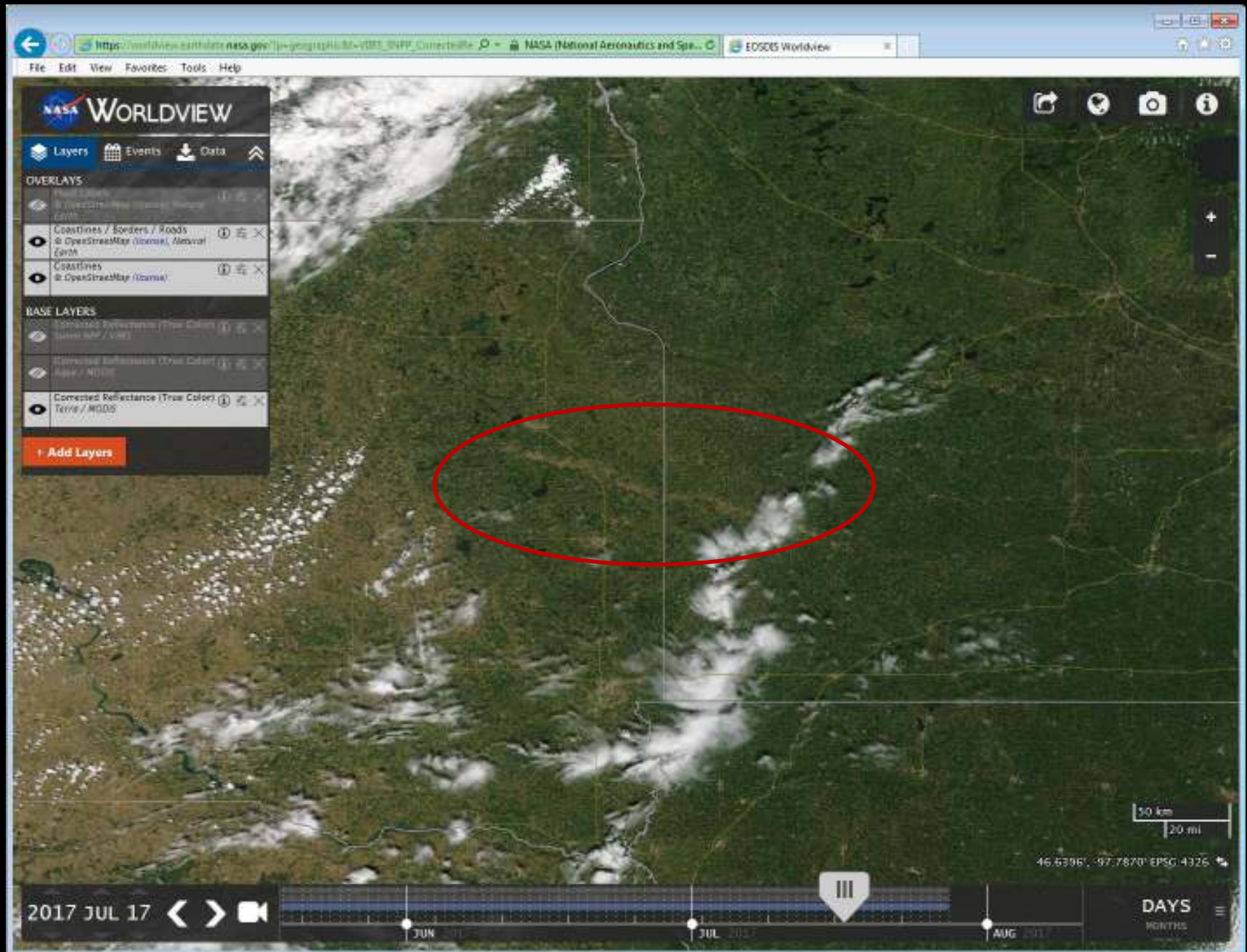
Disciplinary Teams



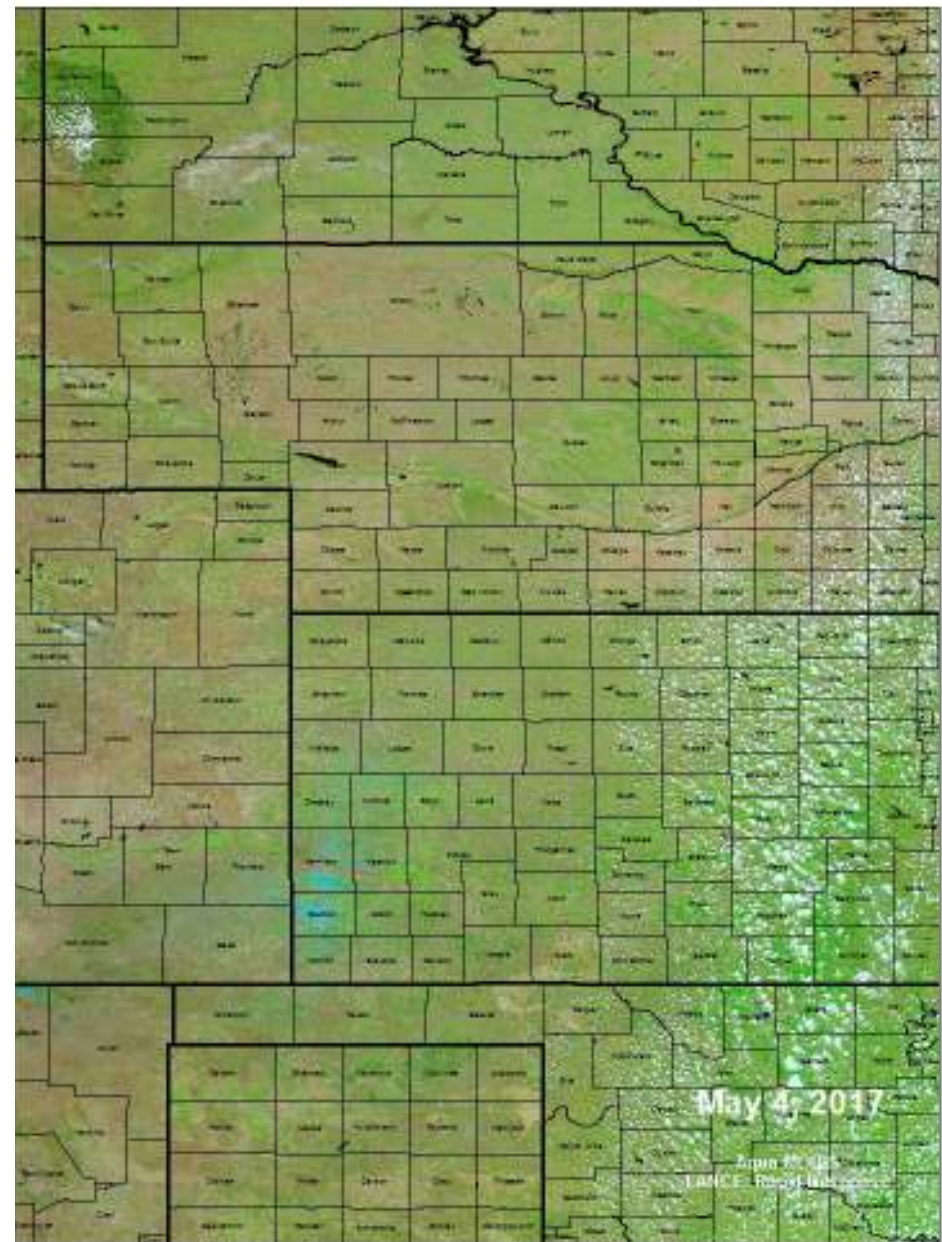
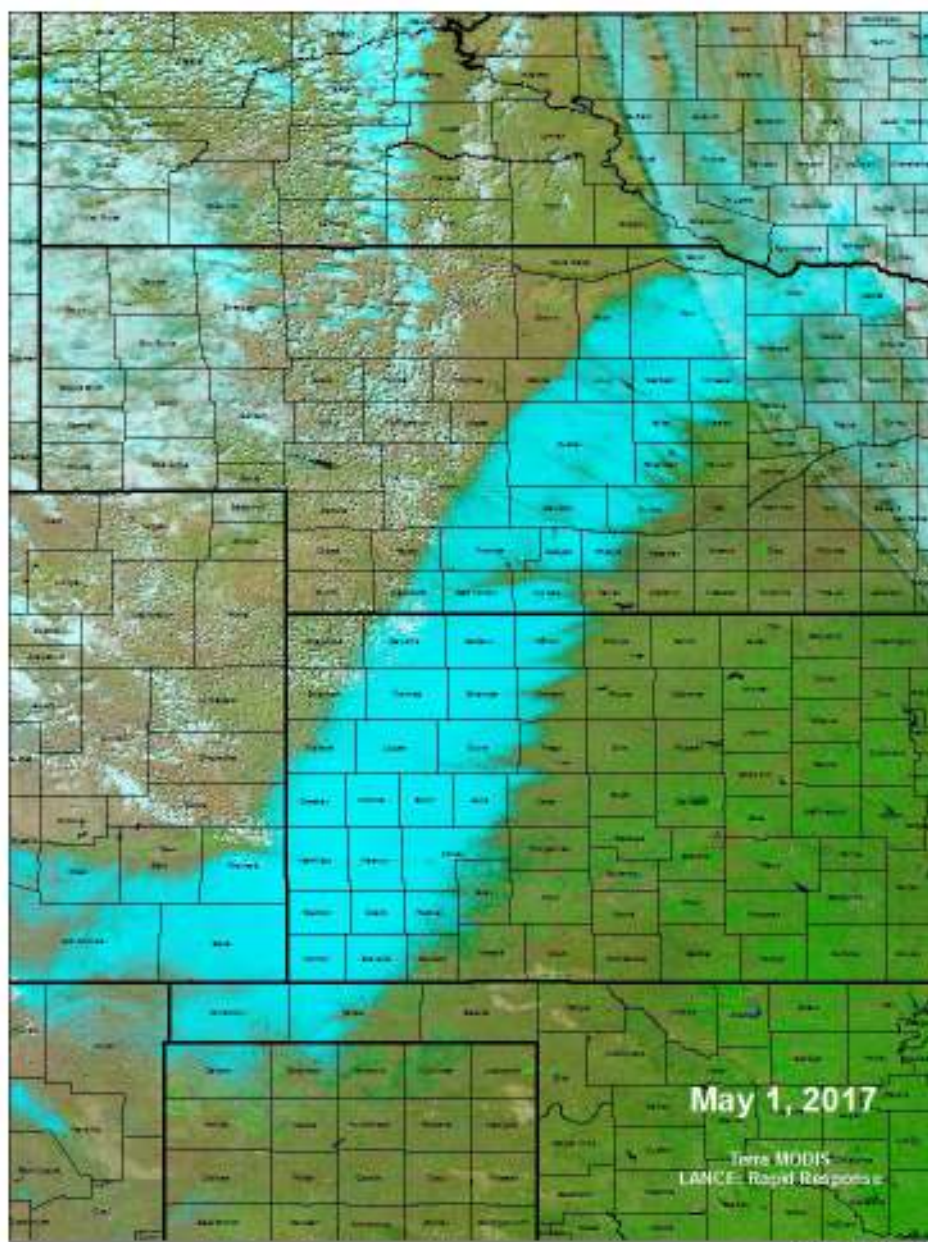
<https://worldview.earthdata.nasa.gov/>



Hail example



MODIS Imagery - Snow event



MODIS Imagery - Flood event



Calculation and use of NDVI

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The Free Encyclopedia

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Normalized Difference Vegetation Index

From Wikipedia, the free encyclopedia

This article **reads more like a story than an encyclopedia entry**. To meet Wikipedia's quality standards and conform to the *neutral point of view* policy, please help to introduce a more formal style and remove any personally invested tone. (July 2011)

The **Normalized Difference Vegetation Index (NDVI)** is a simple graphical indicator that can be used to analyze remote sensing measurements, typically but not necessarily from a space platform, and assess whether the target being observed contains live green vegetation or not.

Contents

- Brief history
- Rationale
- Performance and limitations
- See also
- References
- External links

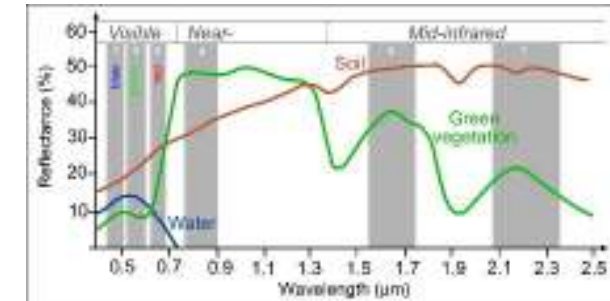
Brief history

The exploration of outer space started in earnest with the launch of Sputnik 1 by the Soviet Union on 4 October 1957. This was the first man-made satellite orbiting the Earth. Subsequent successful launches, both in the Soviet Union (e.g., the Sputnik and Cosmos programs), and in the U.S. (e.g., the Explorer program), quickly led to the design and operation of dedicated meteorological satellites. These are orbiting platforms embarking instruments specially designed to observe the Earth's atmosphere and surface with a view to improve weather forecasting. Starting in 1960, the TIROS series of satellites embarked television cameras and radiometers. This was later (from 1964 onwards) followed by the Nimbus satellites and the family of Advanced Very High Resolution Radiometer instruments on-board the National Oceanic and Atmospheric Administration (NOAA) platforms. The latter measures the reflectance of the planet in red and near-infrared bands, as well as in the thermal infrared. In parallel, NASA developed the Earth Resources Technology Satellite (ERTS), which became the precursor to the Landsat program. These early sensors had minimal spectral resolution, but tended to include bands

Negative values of NDVI (values approaching -1) correspond to water. Values close to zero (-0.1 to 0.1) generally correspond to barren areas of rock, sand, or snow. Lastly, low, positive values represent shrub and grassland (approximately 0.2 to 0.4), while high values indicate temperate and tropical rainforests (values approaching 1).^[1]

average NDVI of June 2000

NDVI in June over the British Isles (NOAA AVHRR)



$$\text{NDVI} = \frac{(\text{NIR} - \text{VIS})}{(\text{NIR} + \text{VIS})}$$

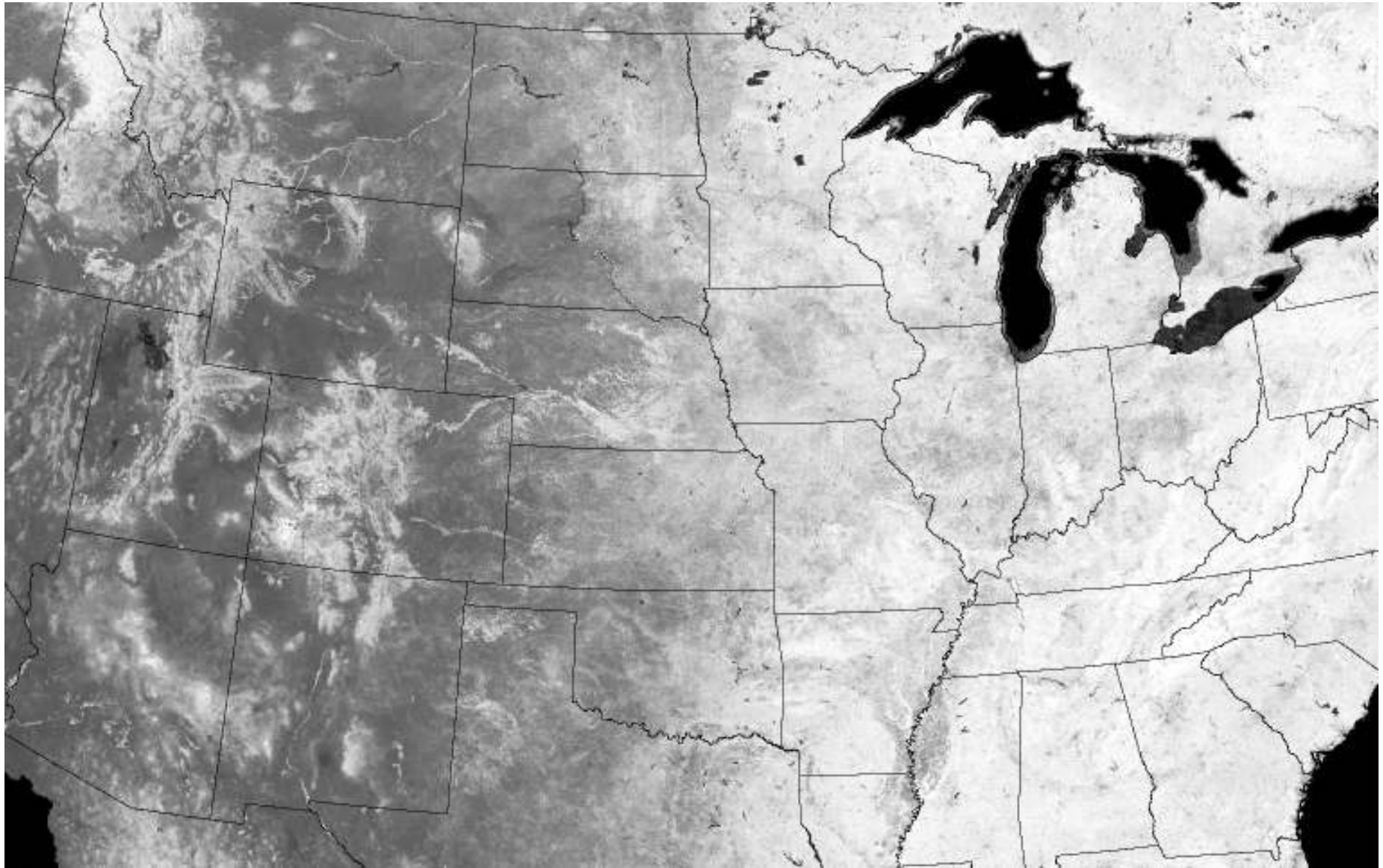
NIR = near-infrared band
VIS = visible band

Ranges from -1.0 to 1.0

NDVI is a related to:

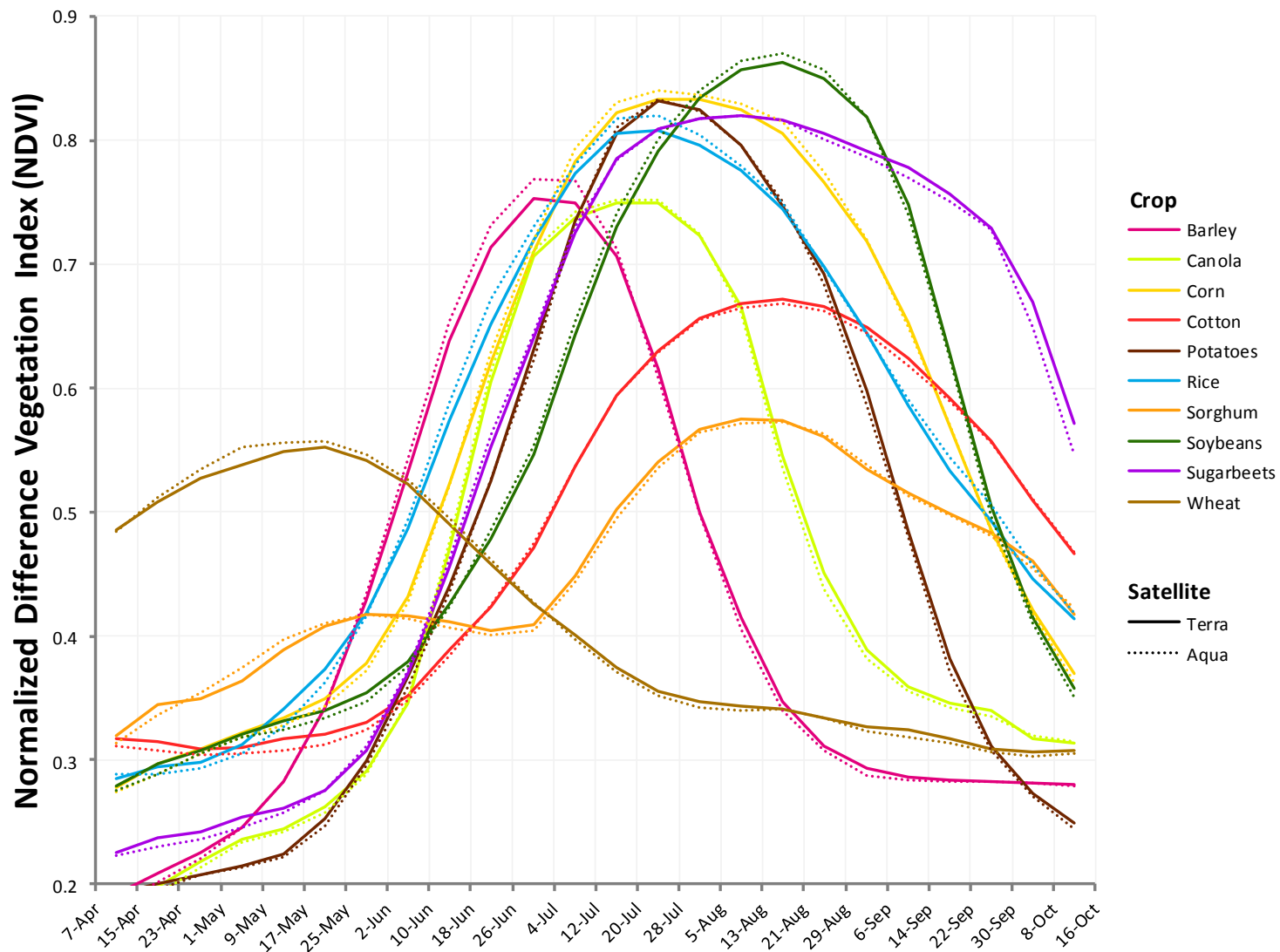
- Plant health
- Chlorophyll content
- “Greenness”
- Amount of Biomass
- Vegetation vigor
- **Yield!**

MODIS NDVI 8-day composite imagery example



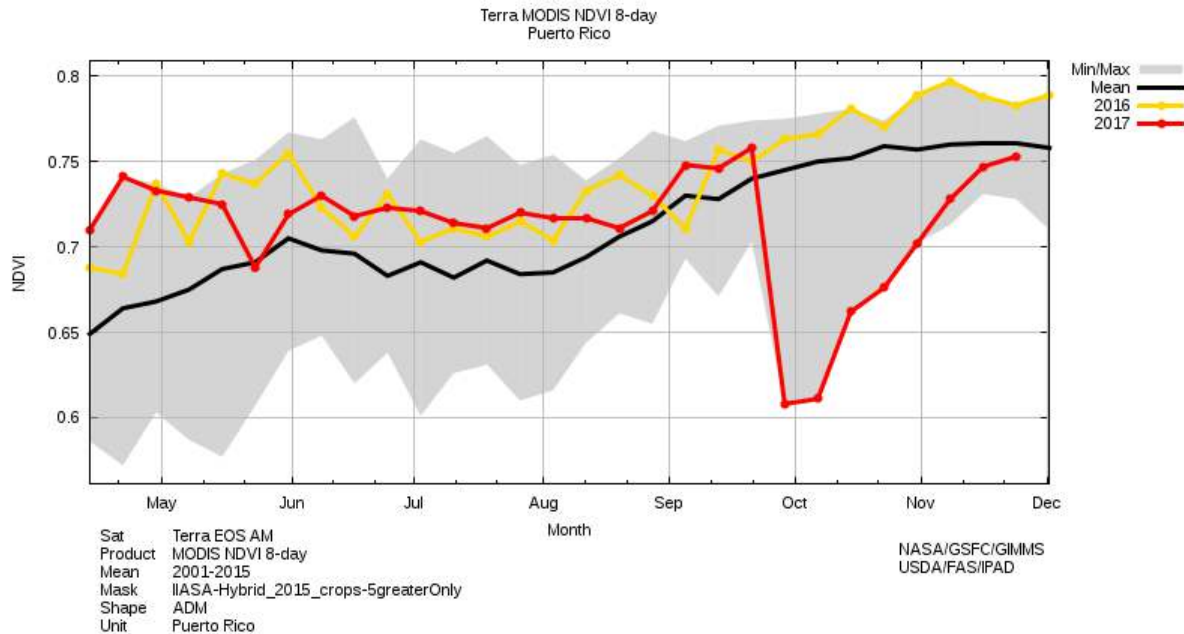
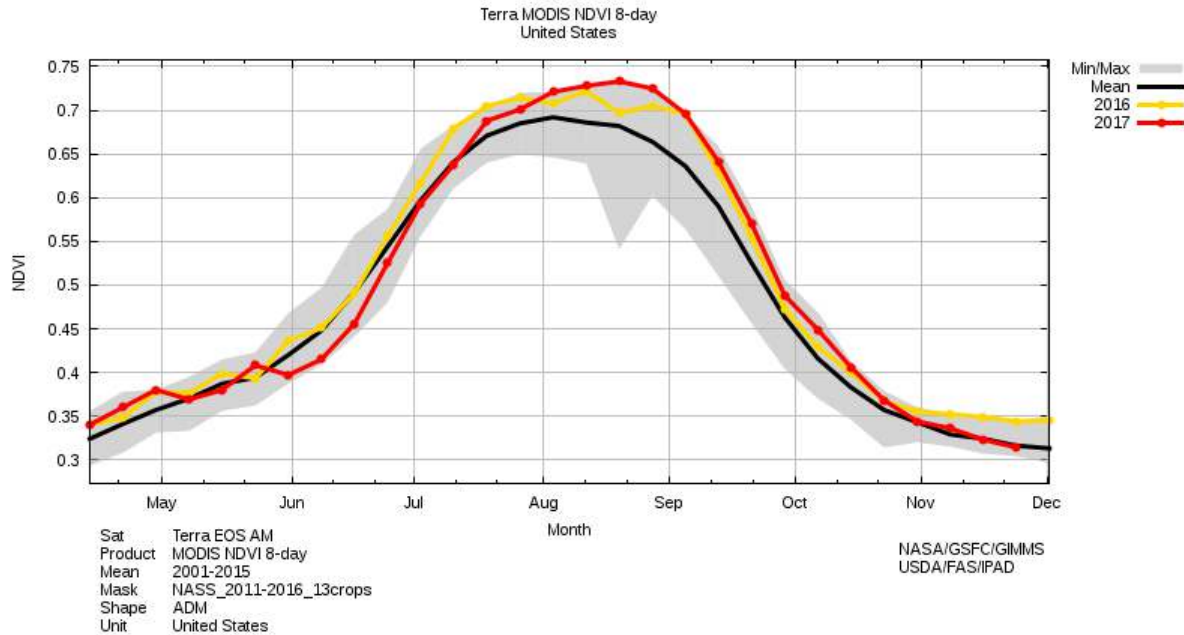
Lighter shades, greater NDVI

Average NDVI phenologies over United States



Signals isolated using crop specific masks

Real-time tracking of NDVI



NASS recent efforts on remote sensing of crop yields

Premise

- Positive relationship between crop yield and biomass – plant vigor - “greenness” - NDVI
- Negative relationship between crop yield and land surface temperature

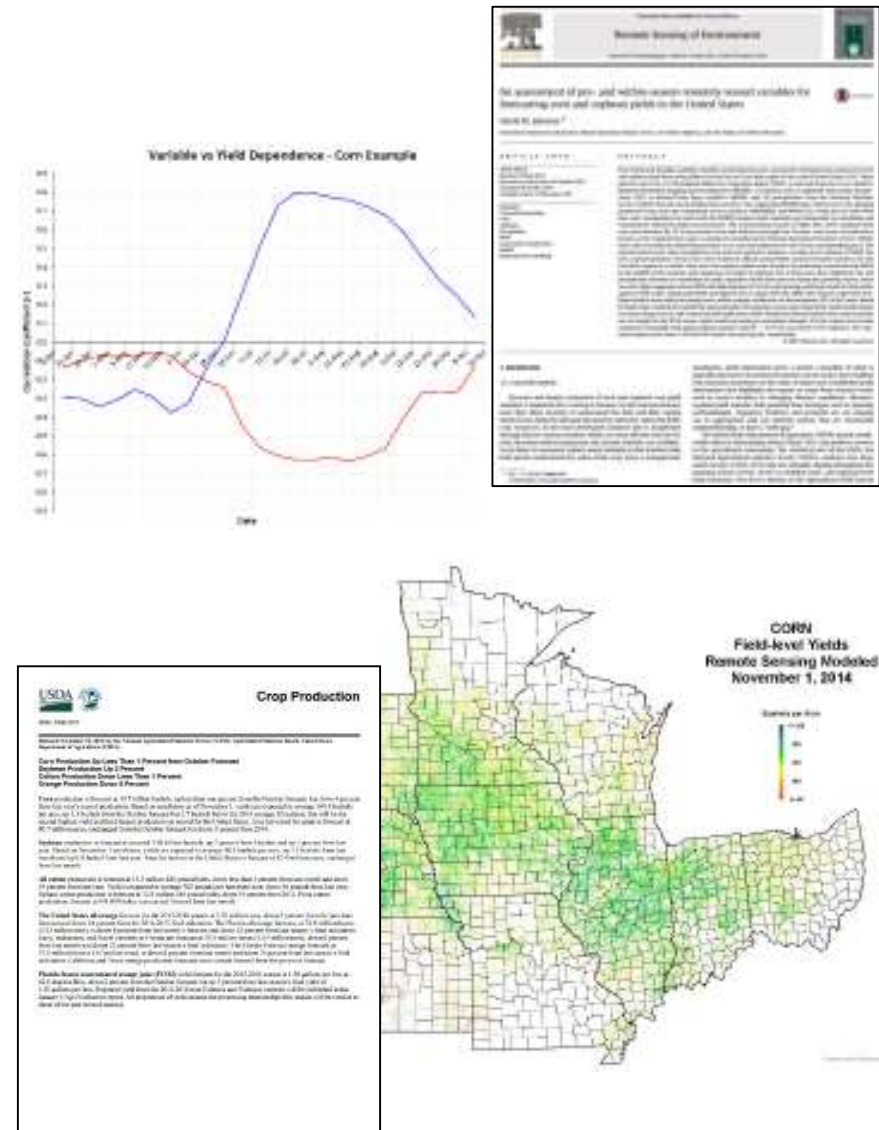
Utilize time-series MODIS satellite data to obtain biomass and temperature estimates throughout the growing season

- Use Cropland Data Layer to isolate known crop areas
- Then use them in an empirically-based prediction model based on historical imagery and NASS county-level yield statistics

Run model at National, State, and County levels

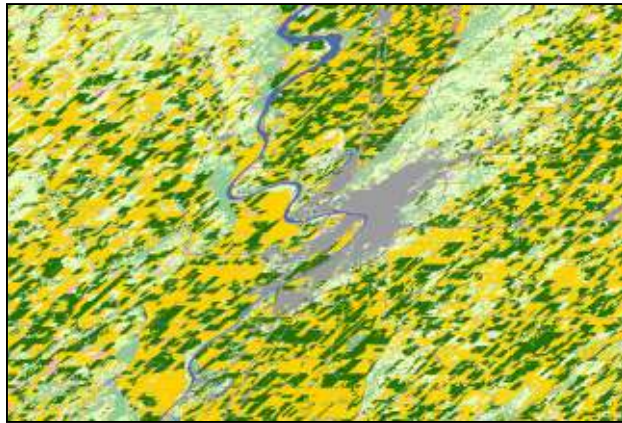
- Integrating over season approach
- Using decision trees (Rulequest Cubist)
- Corn and Soybeans operational currently

Perform within crop season at monthly intervals

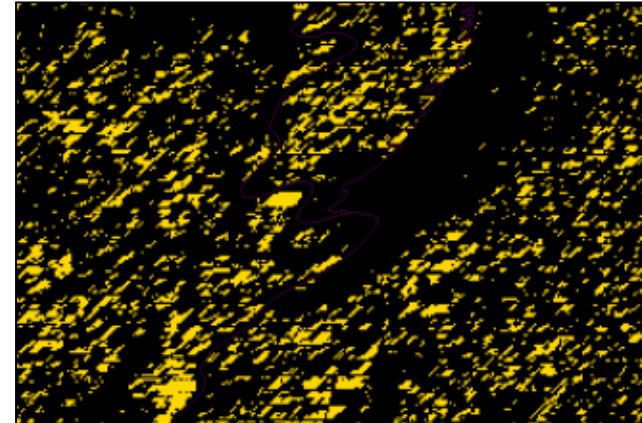


Must be timely, accurate, and useful

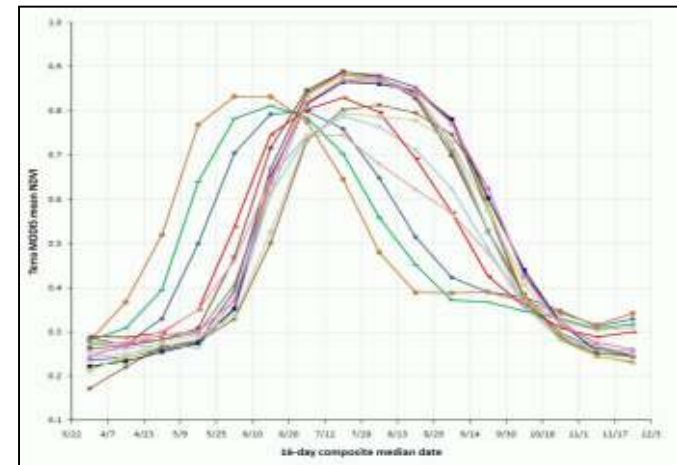
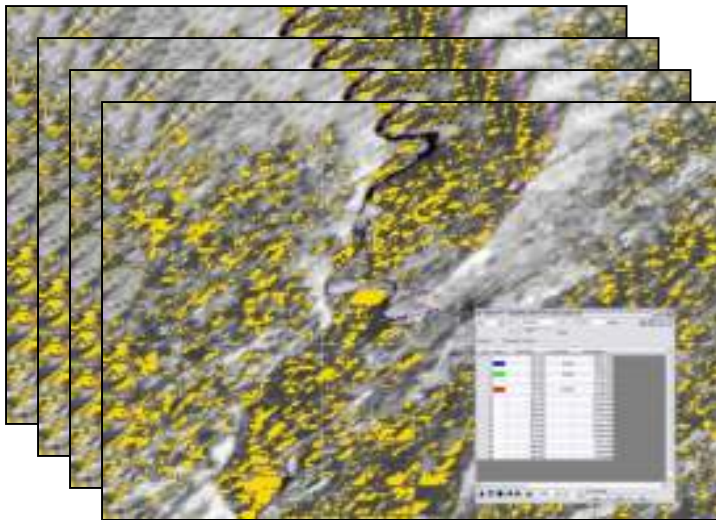
Intersecting of crop “mask” with time-series of MODIS data



CDL



Isolate crop of interest



Intersect crop mask with MODIS time series and then spatially average those pixels

County-level time-series database has been built

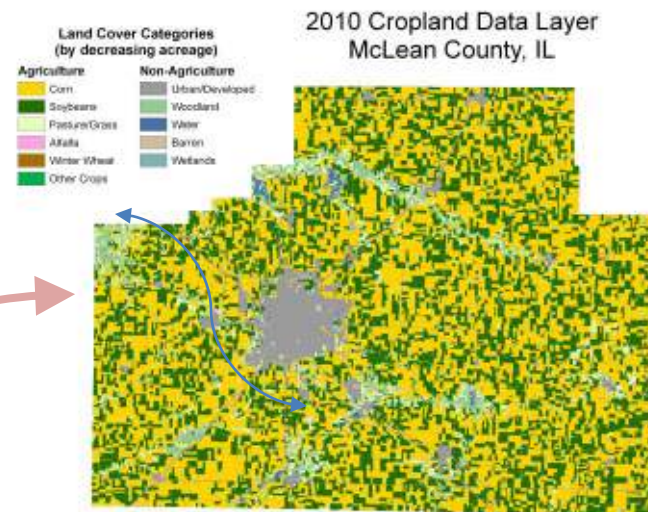
2006 -> present

Every eight day “window” through the growing season

- Observed average value of NDVI
- Observed average value of LST

For every county we also know

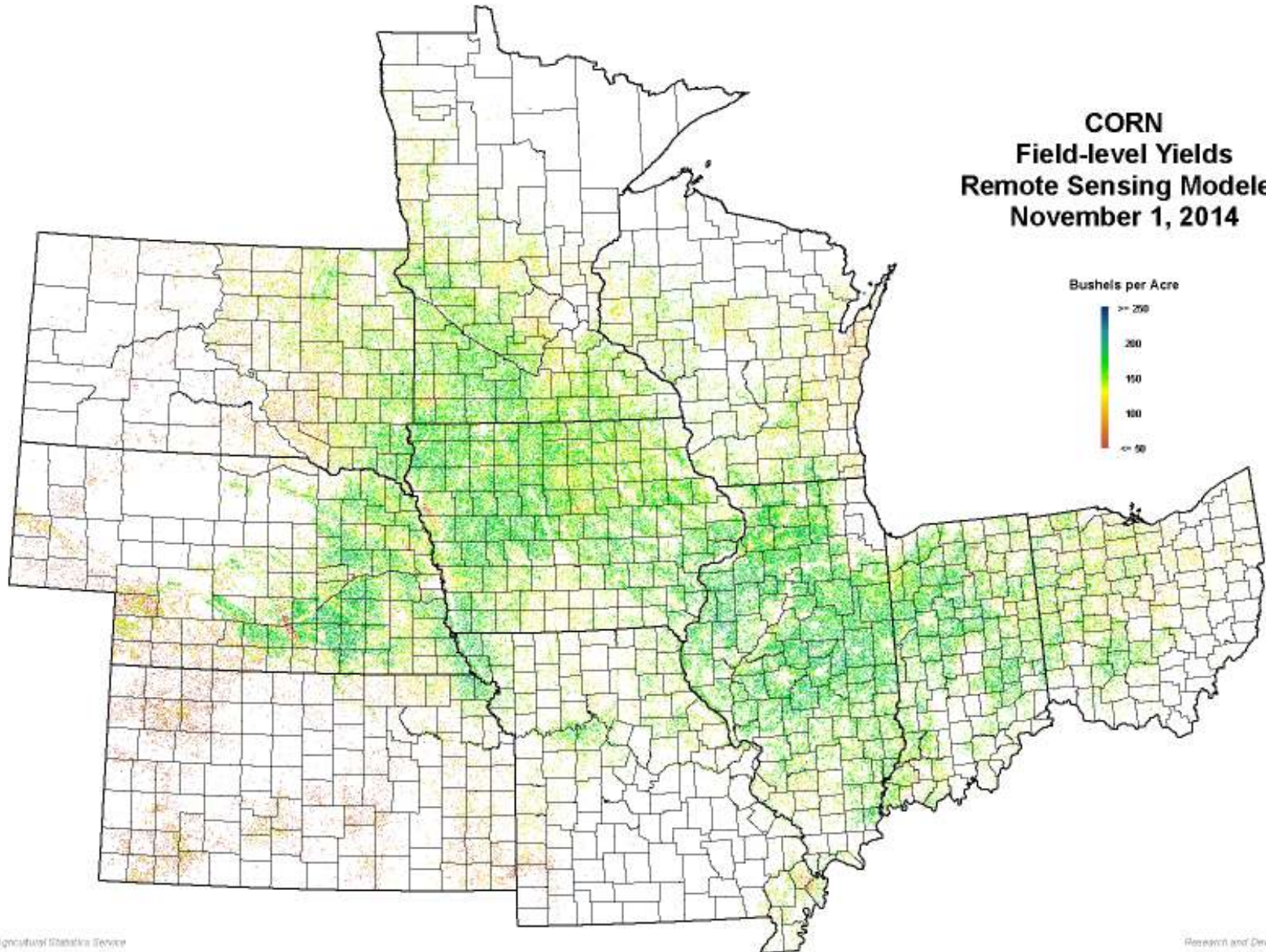
- NASS published yield



state	county	year	yield	NDVI	DLST	23-Apr	1-May	9-May	17-May	25-May	2-Jun	10-Jun	18-Jun	26-Jun	4-Jul	12-Jul	20-Jul
17	93	2010	168.6			2980.673	3264.547	3862.318	3866.409	3990.153	5893.765	7558.422	8108.906	8559.559	8826.817	8930.85	8935.61
17	95	2010	159.9			2992.195	2977.046	3203.401	3377.778	3848.078	5771.909	7450.655	8012.679	8310.476	8537.081	8645.006	8702.09
17	97	2010 ?				3337.864	3836.186	5403.508	4459.949	4311.525	5635.508	7575.966	7776.288	8082.441	8575.966	8689.22	8524.83
17	99	2010	162.9			2844.2	2971.099	3332.757	3486.144	3937.887	6032.626	8059.657	8344.285	8565.456	8784.721	8903.283	8939.18
17	101	2010	156.9			3874.741	3988.952	4349.537	4930.498	5452.197	6205.825	7687.592	8022.794	8396.337	8589.467	8770.097	8827.56
17	103	2010	173.6			2782.144	2805.154	3018.966	3094.823	3512.443	5563.73	7306.284	8102.134	8554.694	8918.413	8949.941	8862.48
17	105	2010	166.6			2816.087	3007.861	3371.65	3608.025	3988.44	6100.426	8236.687	8503.526	8751.071	8872.207	8945.958	8805.10
17	107	2010	155.7			2706.578	2846.325	3249.914	3622.797	4402.778	6661.937	8254.186	8426.524	8515.872	8656.284	8755.741	8782.62
17	109	2010	141.8			3104.659	3240.878	3479.558	3558.215	4056.188	6151.458	7440.174	7913.743	8068.891	8437.704	8697.558	8783.25
17	111	2010	171.4			3079.982	3283.63	3659.725	3626.941	3909.787	5483.311	7163.395	8116.372	8578.756	8844.542	8908.066	8886.72
17	113	2010	169.5			2727.7	2899.42	3316.302	3573.485	4053.523	6484.888	8304.741	8585.89	8846.408	8960.349	8953.985	8860.08
17	115	2010	168.5			2791.229	2943.968	3442.016	3862.389	4880.537	7264.473	8749.776	8793.049	8769.201	8787.036	8828.984	8797.02
17	117	2010	146.9			3213.265	3342.063	3617.414	4030.15	4799.472	6474.308	8021.675	8511.256	8646.314	8885.395	8920.521	9010.37
17	119	2010	166.3			3282.816	3405.388	3712.914	4087.371	4860.512	6581.844	8129.837	8410.098	8587.161	8826.583	8879.477	8854.28
17	121	2010	149.7			3524.353	3534.901	3931.625	4260.018	4856.34	6251.207	7828.069	8242.445	8450.967	8601.465	8853.656	8952.45
17	123	2010	163.3			2748.186	2881.69	3261.708	3448.857	3851.546	5647.397	7541.326	8205.306	8567.037	8799.09	8891.405	8974.80

Map Output

CORN
Field-level Yields
Remote Sensing Modeled
November 1, 2014



USDA/National Agricultural Statistics Service

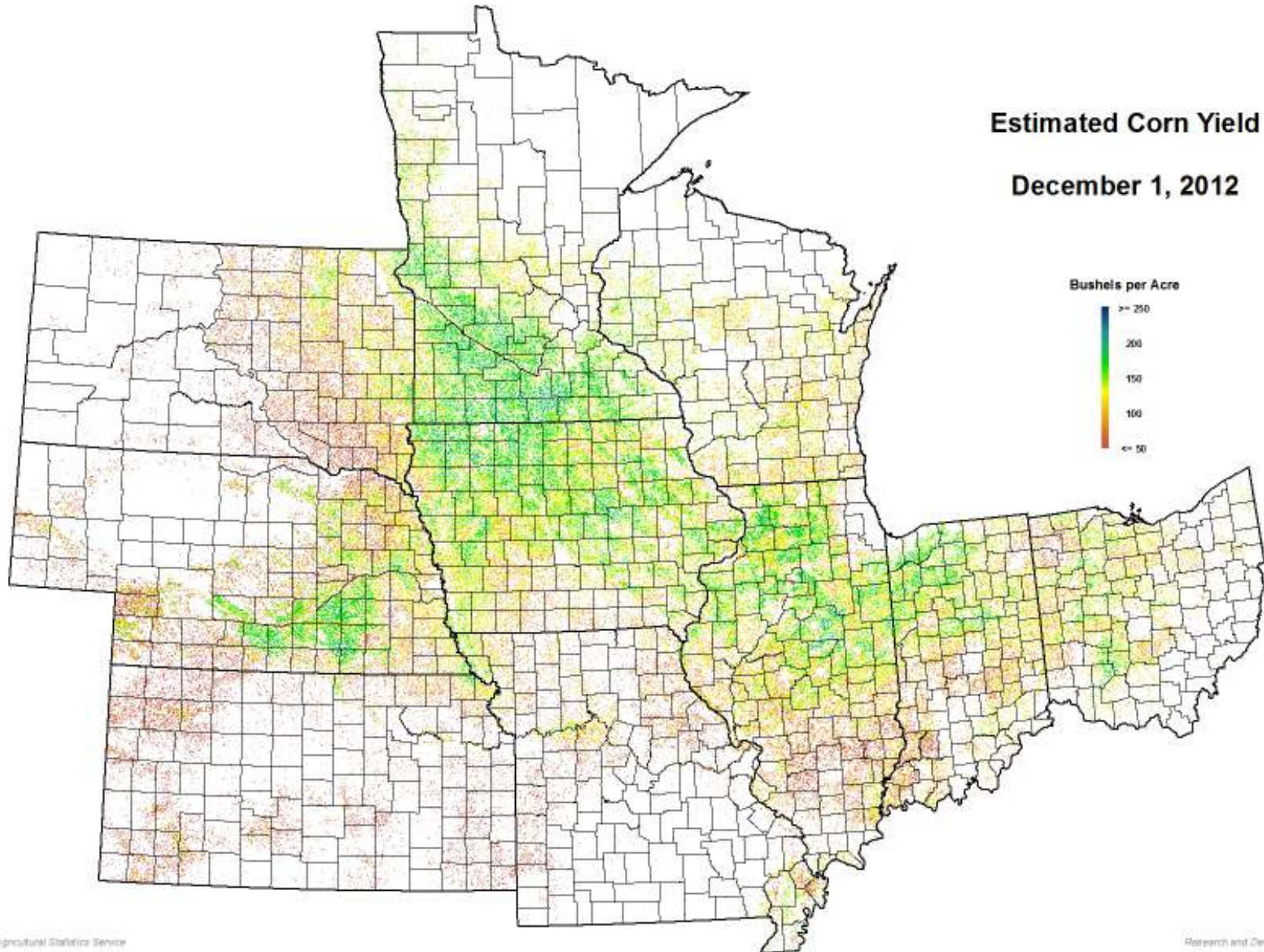
Research and Development Division

Normal year

Map Output

Estimated Corn Yield

December 1, 2012



USDA National Agricultural Statistics Service

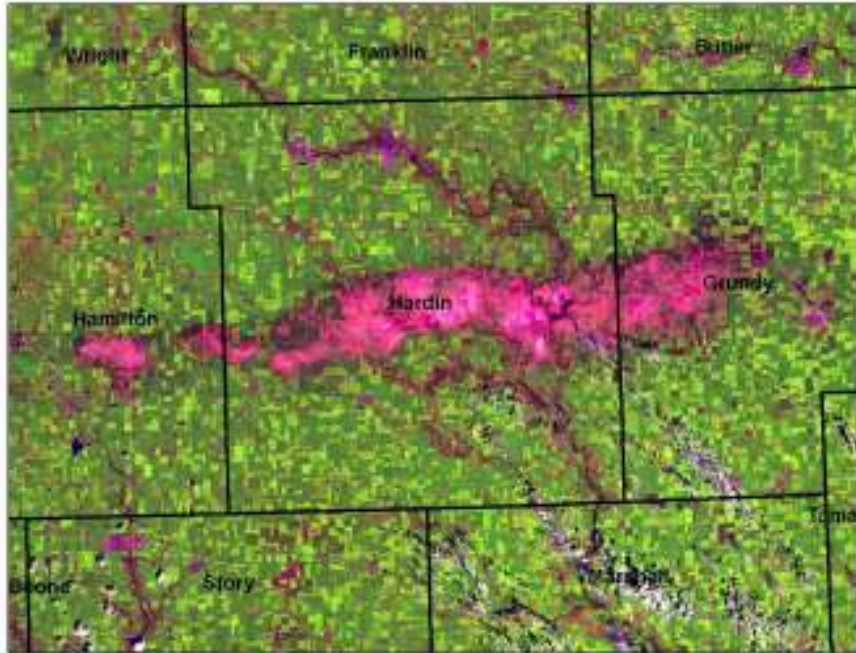
Research and Development Division

Drought year

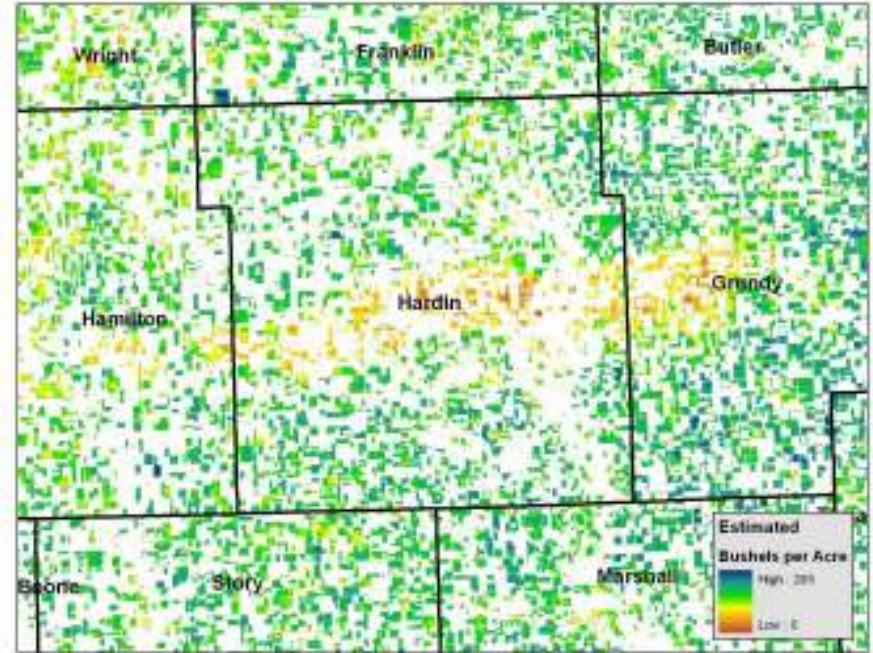
Johnson,³⁷ 2014

Localized example of yield map variability

Scene of a large hailstorm



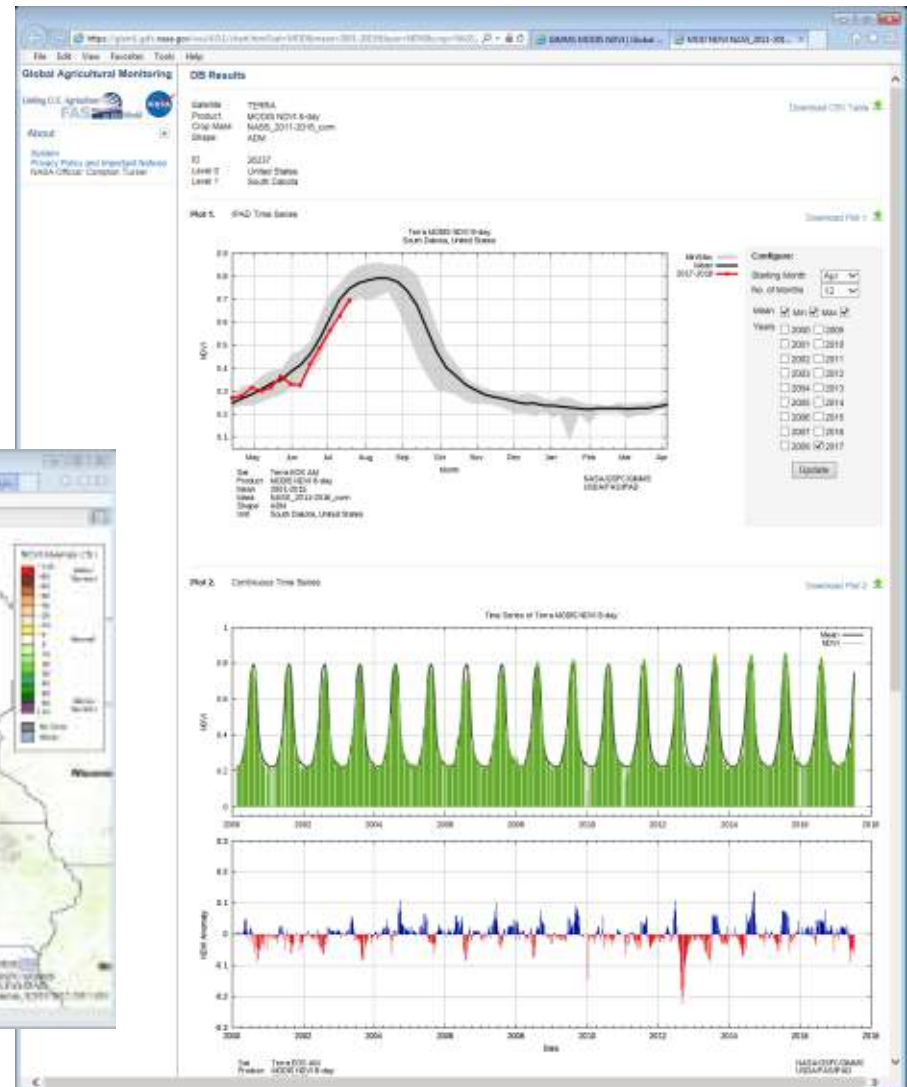
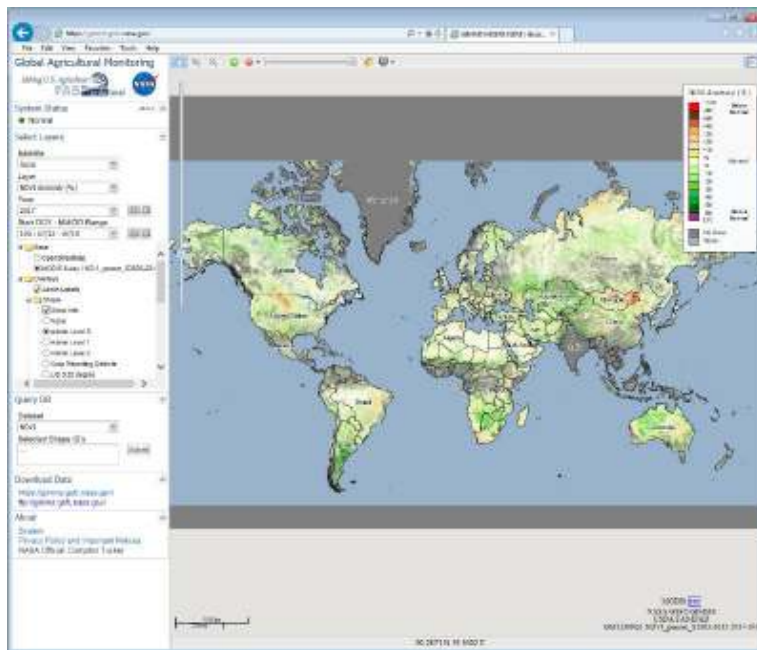
Landsat image



Modeled yields from MODIS

USDA Foreign Agricultural Service/NASA GLAM

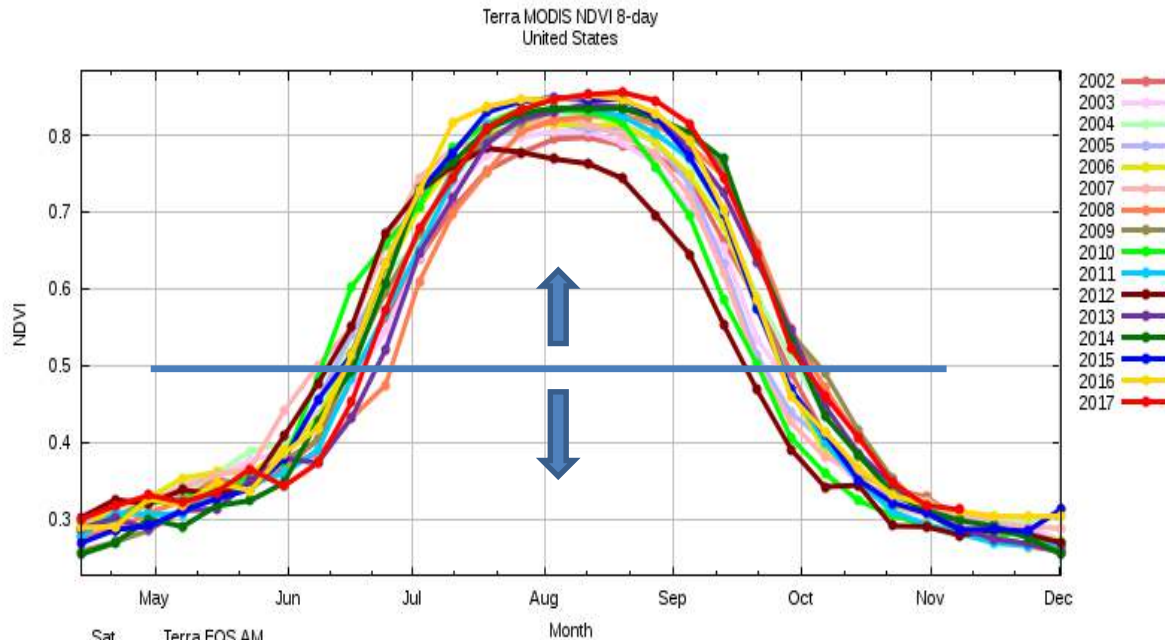
<https://glam1.gsfc.nasa.gov/>



Highly already customized tool for time series analysis and display

Also, shifting to a simpler model construction

Find Optimal
Threshold Value

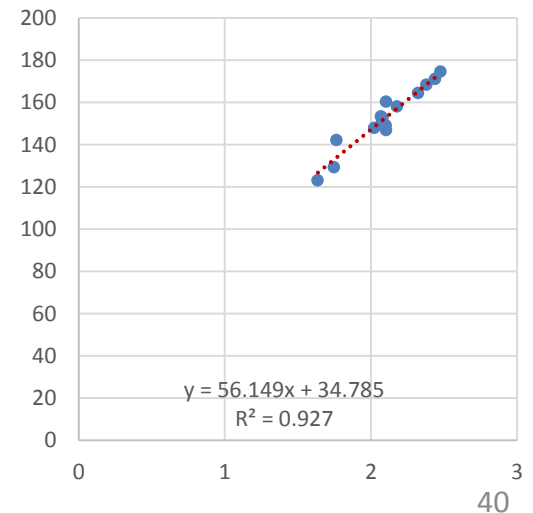


Sat Terra EOS AM
Product MODIS NDVI 8-day
Mean 2001-2015
Mask NASS_2011-2016_corn
Shape ADM
Unit United States

NASA/GSFC/GIMMS
USDA/FAS/IRPAD

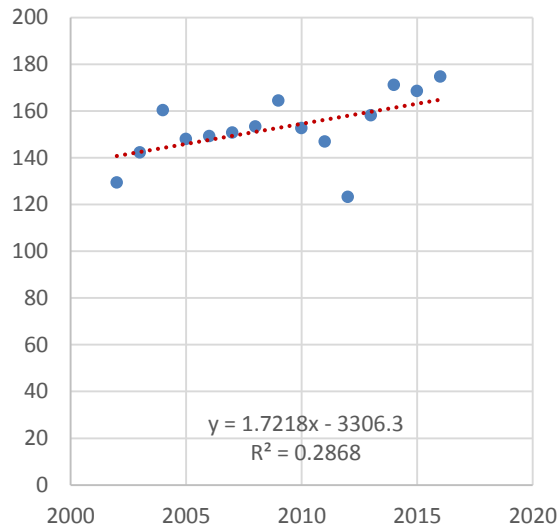
Calculate area under the
curve, over a threshold
and relate to past years.

year	yield	andvi
2002	129.3	1.749
2003	142.2	1.765
2004	160.3	2.106
2005	147.9	2.024
2006	149.1	2.104
2007	150.7	2.08
2008	153.3	2.07
2009	164.4	2.324
2010	152.6	2.082
2011	146.8	2.105
2012	123.1	1.637
2013	158.1	2.179
2014	171	2.44
2015	168.4	2.382
2016	174.6	2.477



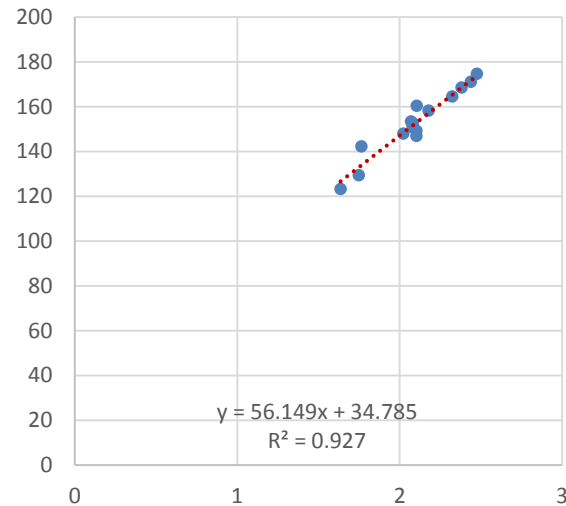
USA national-level simplistic corn yield model

Trend



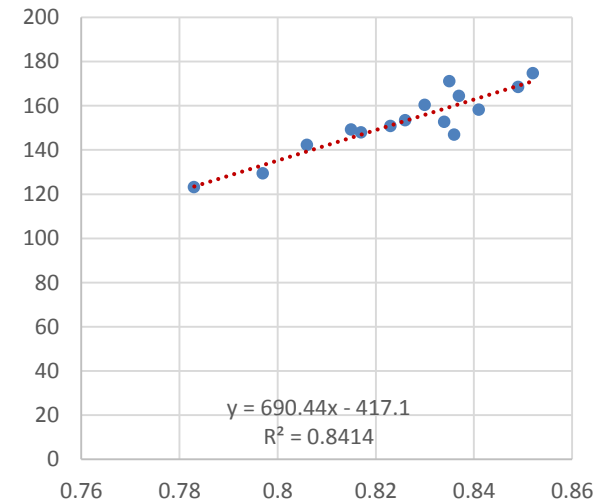
Standard Error 12.5996

Integrate



Standard Error 4.0309

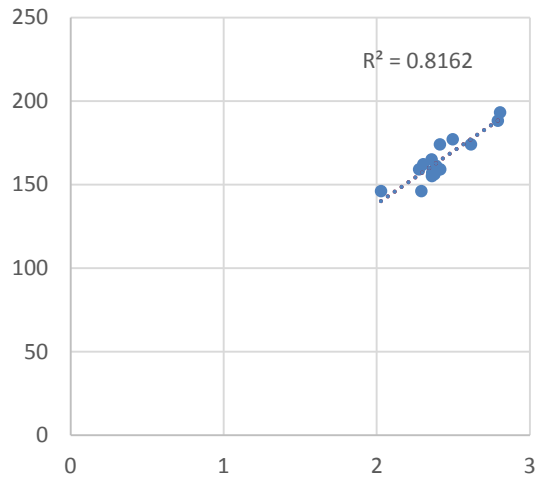
Max



Standard Error 5.9422

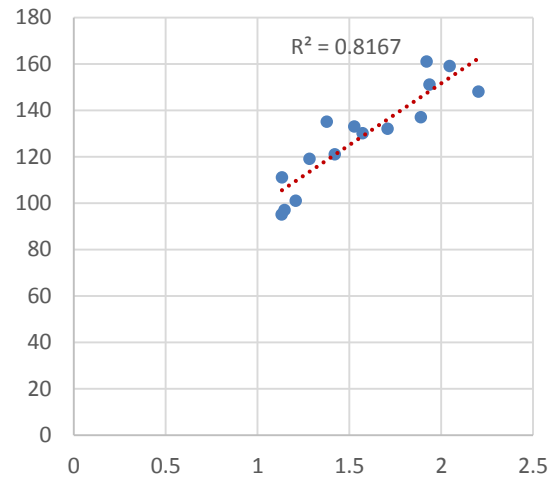
State-level simplistic yield modeling

Minnesota



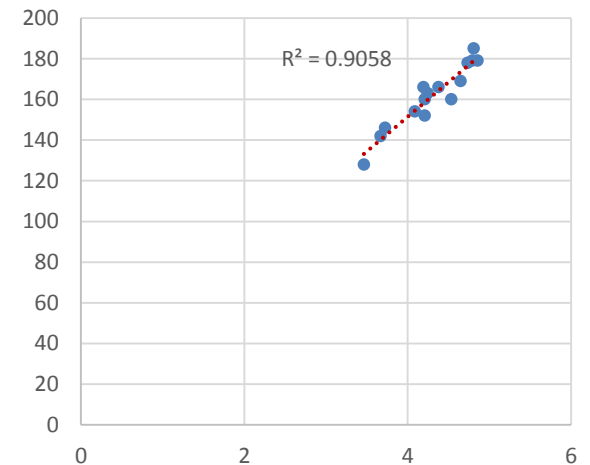
Standard Error 6.1590

South Dakota



Standard Error 9.4601

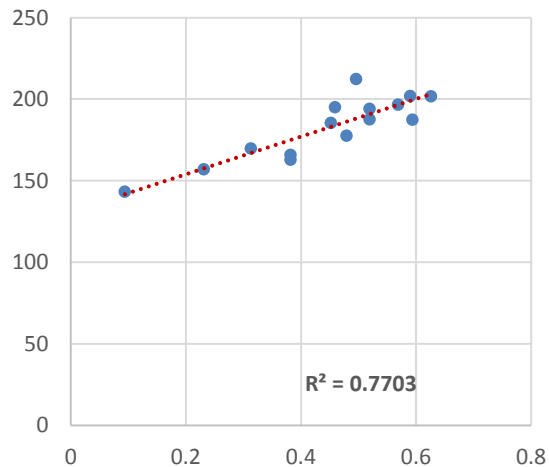
Nebraska



Standard Error 4.9836

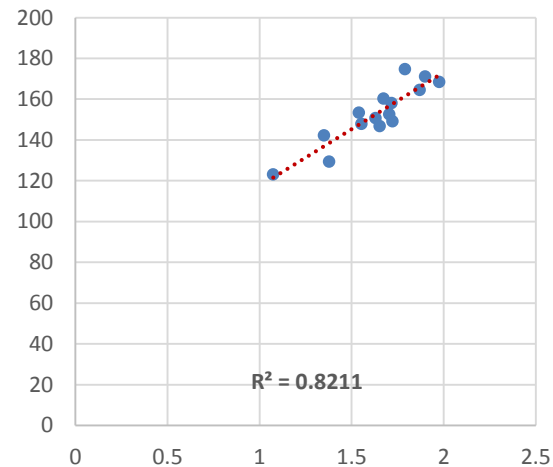
County-level simplistic yield modeling

Sioux, Iowa



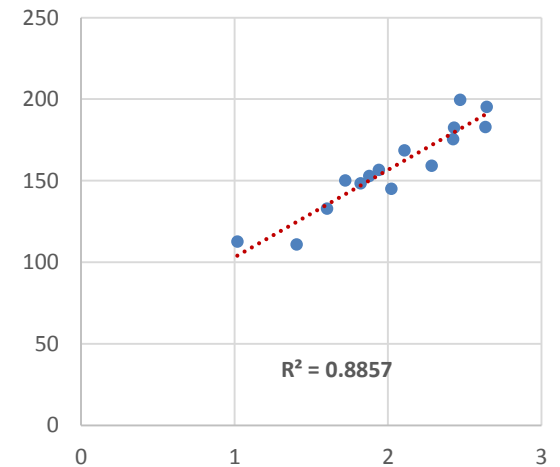
Standard Error 10.41041

Minnehaha, South Dakota



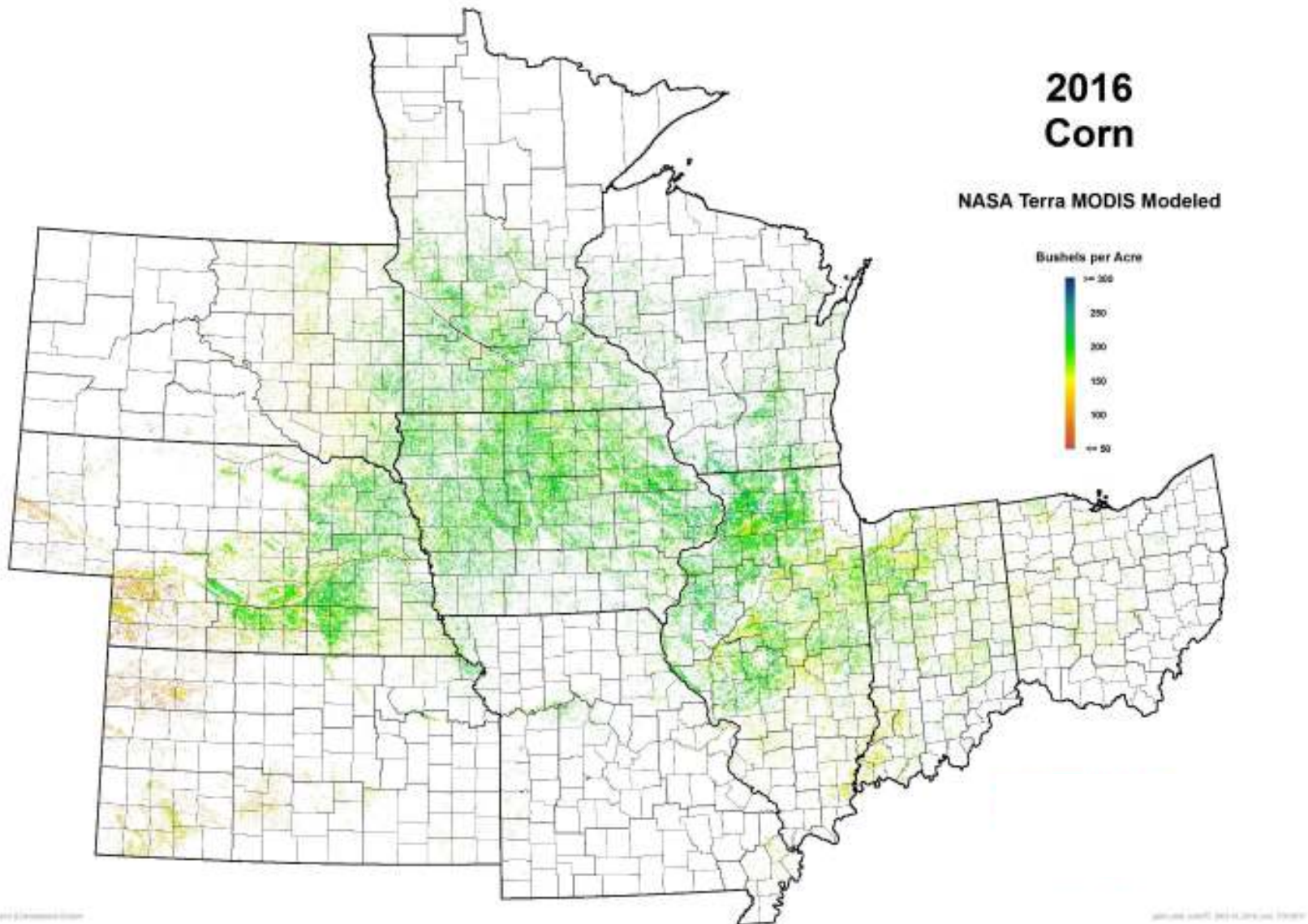
Standard Error 6.31143

Madison, Nebraska

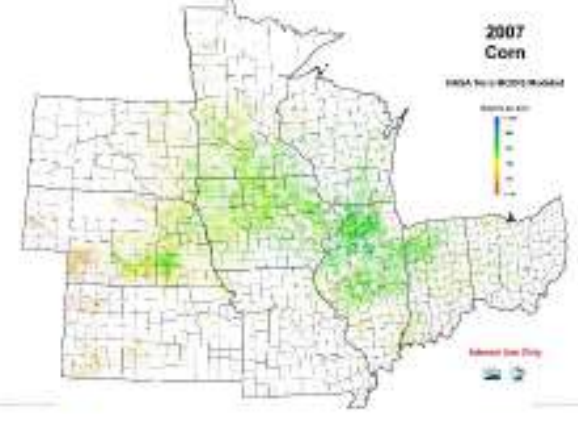
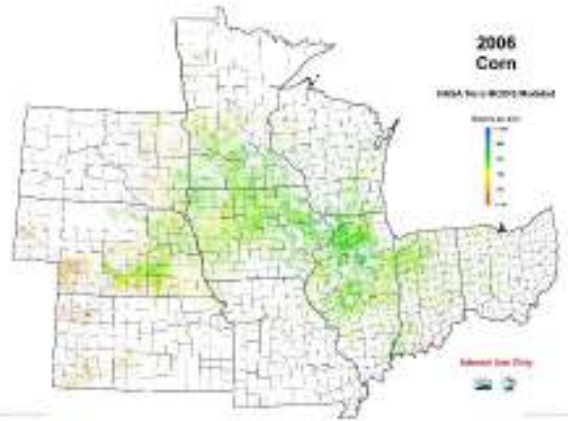
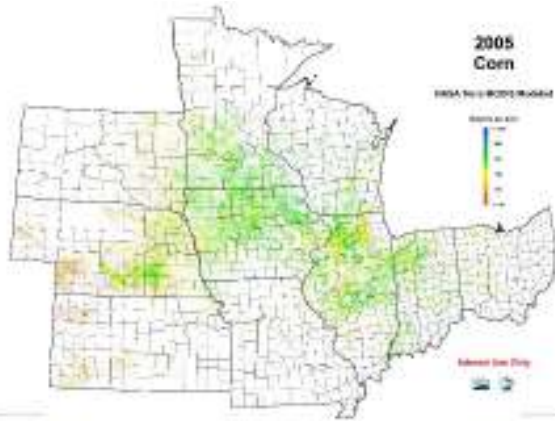
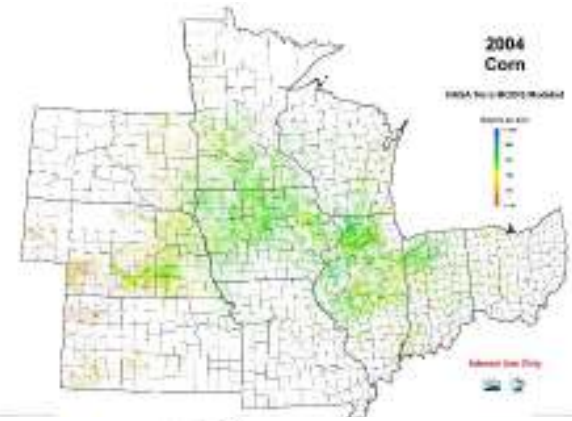
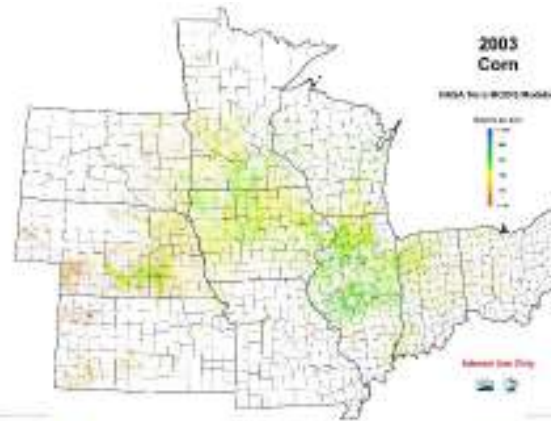


Standard Error 9.377654

Map output still possible



And easy to create time series...



Summary of Remote Sensing for Crop Production Estimation

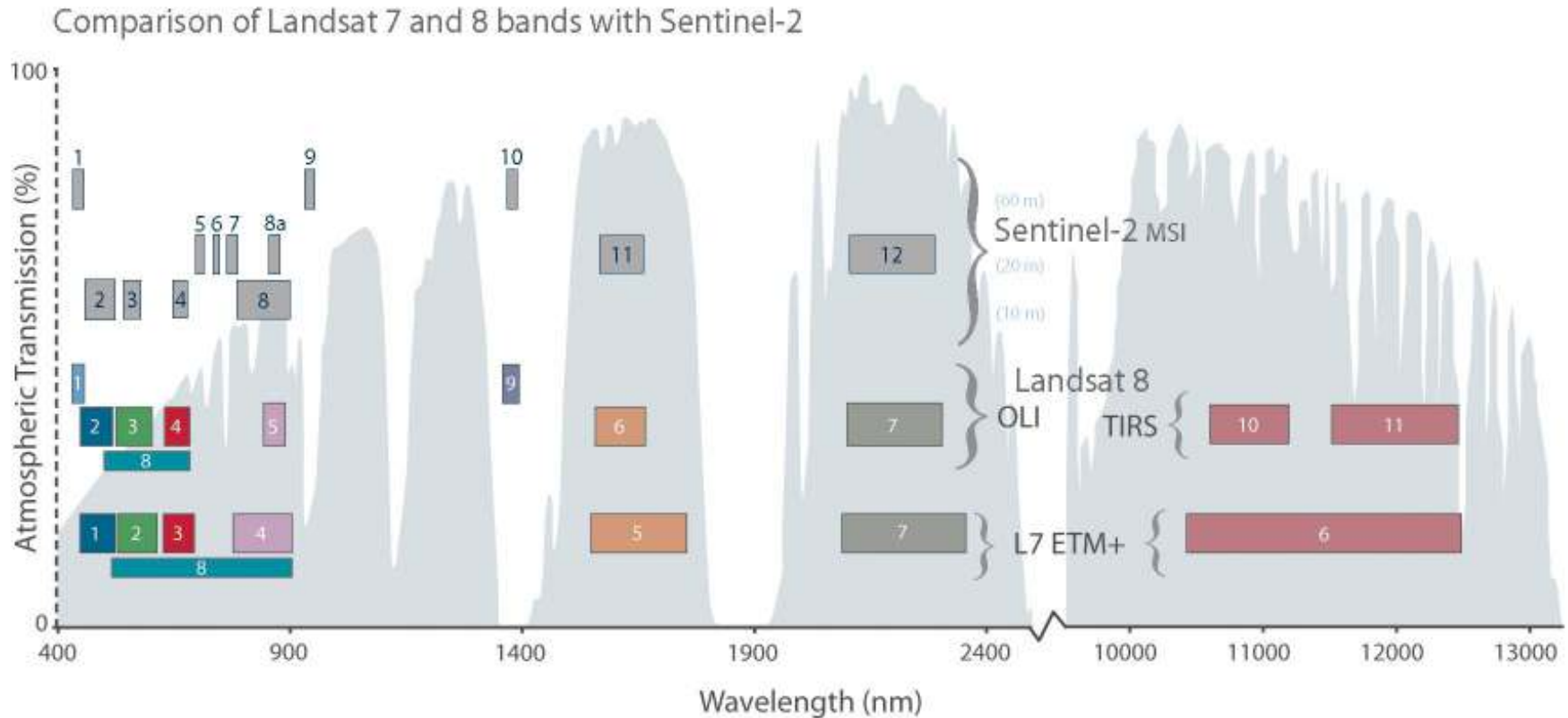
- **Strengths**

- Good areal coverage
- Solid temporal coverage
- Many free data sources
- Better sensors on the way
- Little data latency
- Fine spatial detail
- Simple statistical models seem to be as good as complicated ones
- Cheap computing and analytics has been a boon

- **Weaknesses**

- Computationally intensive
- Integrative skill set required
- Calibration of datasets always ongoing
- Measurement uncertainties difficult to quantify
- A variety of noise sources are present
- No long-term history
- *In situ* validation lacking
- Past utility was oversold

Sentinel-2 vs Landsat 7 & 8 spectral bands



Acreage estimate for a crop in stratum h

$$\hat{y}_h = N_h[\bar{y}_h + b_h(\bar{X}_h - \bar{x}_h)]$$

N_h = Number of frame units(segments in frame)

\bar{y}_h = **sample** mean per segment of reported acres of crop cover

b_h = Slope of the regression of acres in segment on pixel(acres)

\bar{X}_h = **population** mean pixels(acres)in segment

\bar{x}_h = **sample** mean pixels(acres)in segment

Estimate of county total for a crop, stratum

$$\hat{T}_{(BF)_{hc.}} = N_{hc} [\hat{\beta}_{0h} + \hat{\beta}_{1h} \bar{x}_{hc} + \delta_{hc} \bar{u}_{hc.}]$$

$$\bar{u}_{hc.} = \bar{y}_{hc.} - \hat{\beta}_{0h} - \hat{\beta}_{1h} \bar{x}_{hc.} \quad (\text{residual})$$

- 1) if $\sigma^2_{\text{within}} = 0$, use $\delta = 1$,
- 2) if $\sigma^2_{\text{between}} = 0$, use $\delta = 0$,
- 3) if < 2 segments use $\delta = 0$,
- 4) if $\sigma^2_{\text{within}} = 1.0$, use $\delta = 0$,
- 5) otherwise use $\delta = \gamma$